

Real-Time Communication

- Integrated Services: Integration of variety of services with different requirements (real-time and non-real-time)
- Traffic (workload) characterization
- Scheduling mechanisms
- Admission control / Access control (policing)
- Deterministic vs. stochastic analysis
 - Traffic characterization
 - Performance guarantees
- Later we will
 - talk about real-time communication management in the real-world (intserv, some diffserv)
 - wrap up things with a theoretical framework (network calculus)

© R. Bettati

Providing Real-Time Guarantees

sender application

receiver application

→

network service

←

Traffic Specification

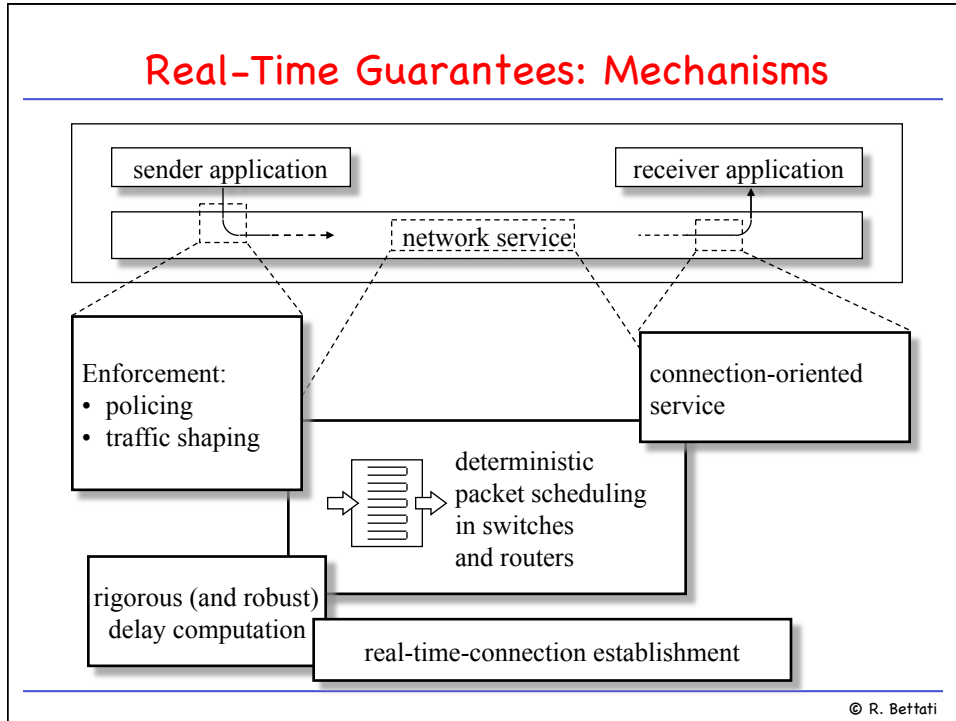
- packet sizes
- packet inter-arrival times
- general traffic descriptors

Performance Requirements

- delay
- bandwidth
- jitter
- packet loss

As long as the traffic generated by the sender does not exceed the specified bounds, the network service will guarantee the required performance.

© R. Bettati

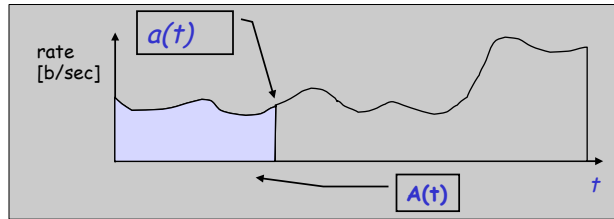


Real-Time Communication

- Integrated Services: Integration of variety of services with different requirements (real-time and non-real-time)
- Traffic (workload) characterization
- Scheduling mechanisms
- Admission control / Access control (policing)
- Deterministic vs. stochastic analysis
 - Traffic characterization
 - Performance guarantees
- Later we will
 - talk about real-time communication world (intserv, some diffserv)
 - wrap up things with a theorem

© R. Bettati

Traffic Description: Traffic Bounding Functions



Arrival as stochastic process
 $A = \{A(t), t \geq 0\}$

A and a are poor traffic descriptors:
 - time dependent

Deterministic traffic arrival descriptors (time-independent)
 Maximum Traffic Function $b(I) \geq \max_{t \geq 0} \{A(t+I) - A(t)\}$
 Maximum Rate Function $b(I)/I \geq \max_{t \geq 0} \{A(t+I) - A(t)\}/I$

© R. Bettati

Traffic Bounding Function $b(.)$

Let $b(.)$ be a monotonically increasing function.

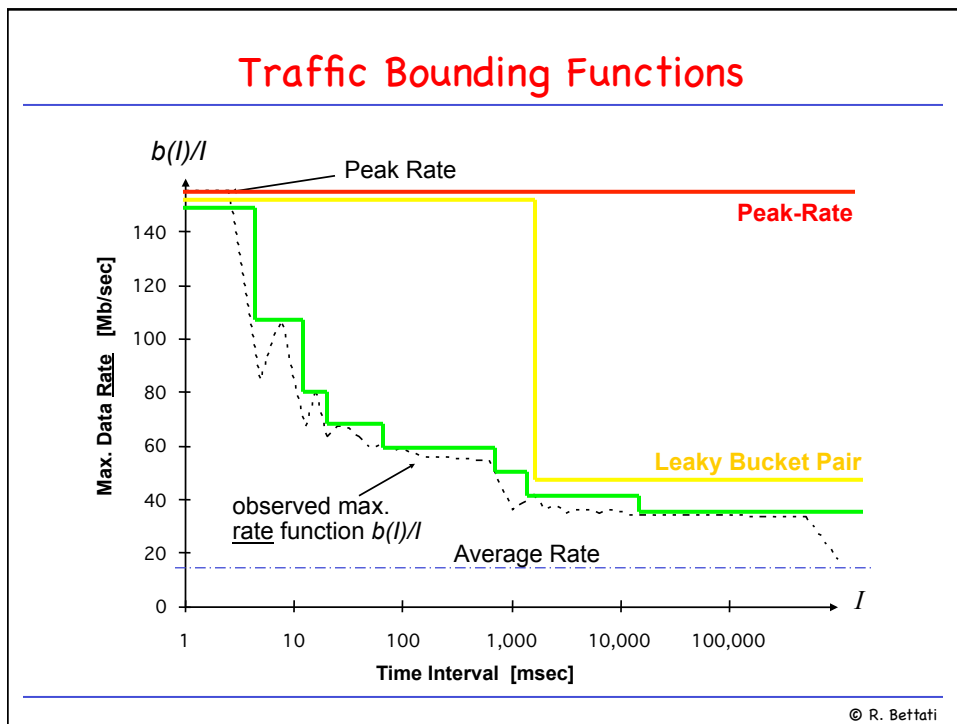
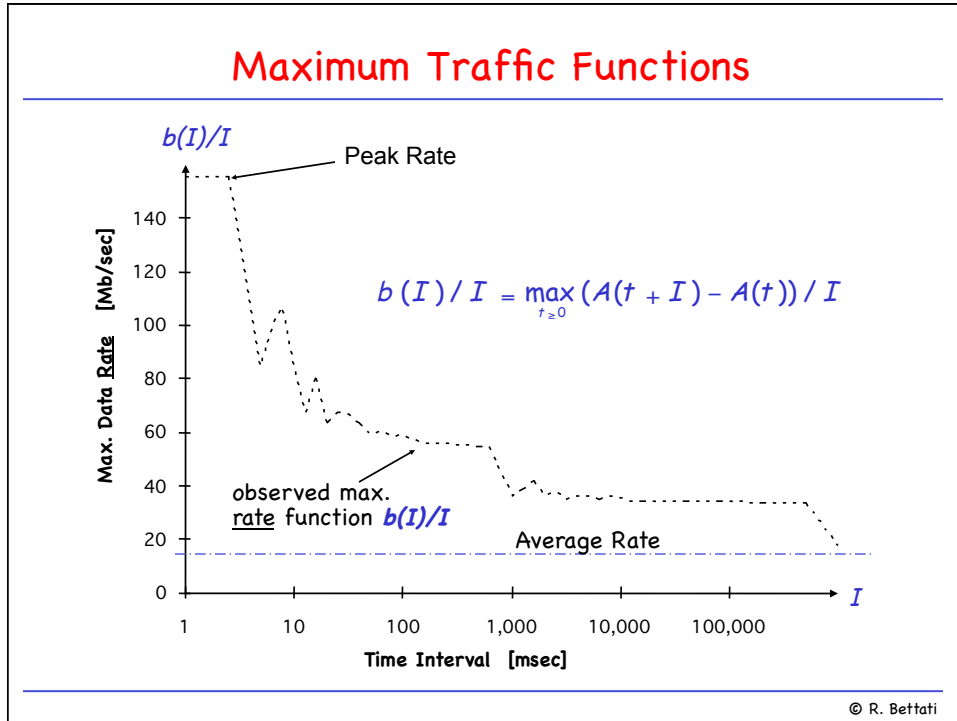
We call $b(.)$ a **deterministic traffic constraint function** of a connection if during **any** interval of length I , the number of bits arriving during the interval is no greater than $b(I)$.

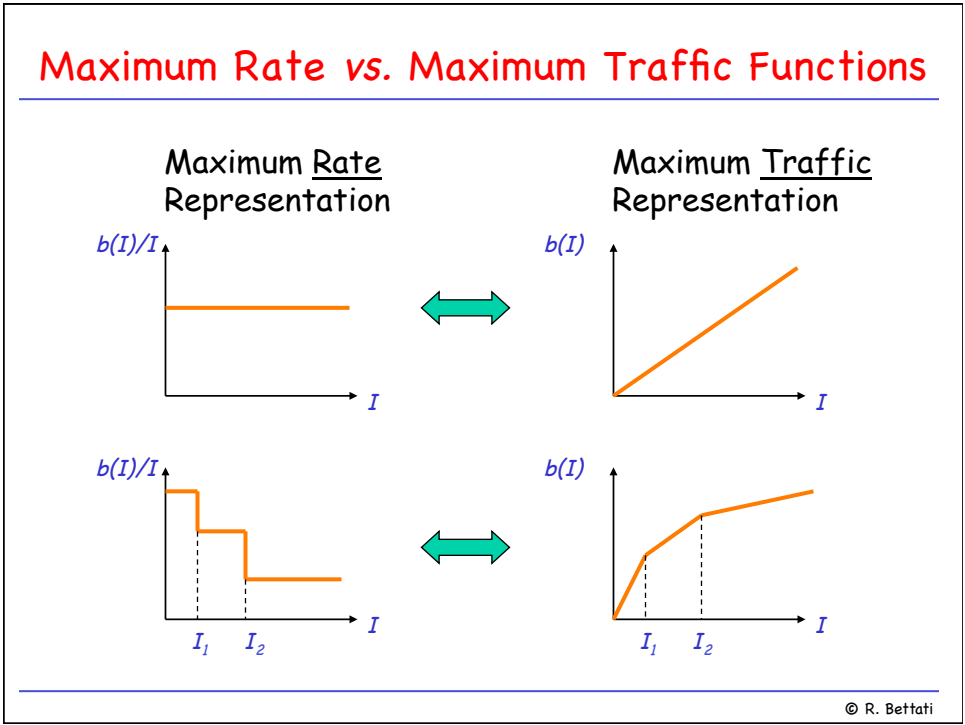
Let $A[t_1, t_2]$ be the number of packets arriving during interval $[t_1, t_2]$. Then, $b(.)$ is a traffic constraint function if

$$\forall s, I > 0, \quad A[s, s + I] \leq b(I)$$

- Traffic models inherently define a traffic constraint function.
- The accuracy of models can be compared by comparing their constraint functions.

© R. Bettati





- ### Traffic Models
- Deterministic Models:**

 1. Periodic model: (e, ρ)
 2. Deferred Server, Sporadic Server model: (e_s, ρ_s)
 3. (σ, ρ) model [Cruz]
 4. Leaky bucket model [Turner, ...]: (β, ρ)
 5. $(x_{min}, x_{aver}, I, s_{max})$ model [Ferrari & Verma]
 6. D-BIND model (Deterministic Bounding Interval Length Dependent) [Knightly & Zhang]
 7. Γ -functions [Zhao]
- Probabilistic Models:**

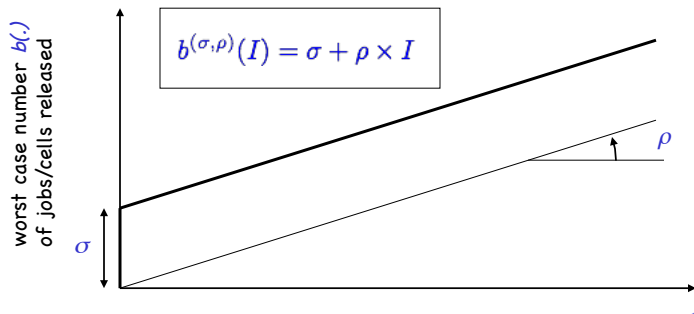
 1. S-BIND model (Stochastic Bounding Interval) [Knightly]
 2. Markov-Modulated Poisson Processes
- © R. Bettati

Cruz' (σ, ρ) Model

"If the traffic is fed to a server that works at rate ρ while there is work to be done, the size of the backlog will never be larger than σ ."

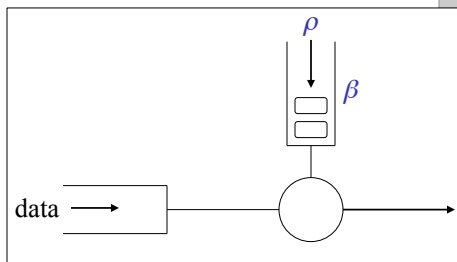
IOW:
The number of jobs/cells released during any interval I does not exceed $\rho I + \sigma$.

Graphical representation:

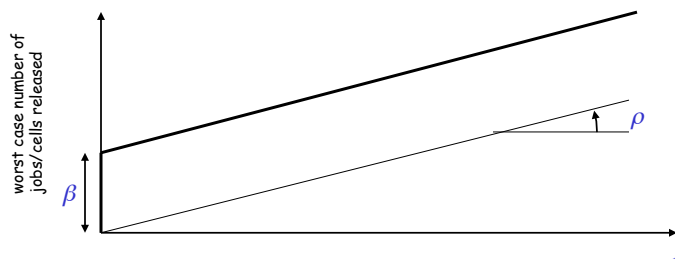


© R. Bettati

The Leaky Bucket Model



- Implementation:
 - Maintain counter for each traffic stream.
 - Increment counter at rate ρ , to maximum of β .
 - Each time a packet is offered, the counter is checked to be > 0 .
 - If so, decrement counter and forward packet; otherwise drop packet.



© R. Bettati

Concatenating Leaky Buckets

Q: What about limiting the maximum cell/frame rate?

The graph plots the worst case number of jobs/cells released against the number of jobs/cells x . The function consists of two linear segments. The first segment starts at the origin with a slope of ρ_2 and a vertical offset of β_2 . The second segment starts at a point (x_1, y_1) with a slope of ρ_1 and a vertical offset of β_1 relative to the extension of the first segment.

The diagram shows two leaky buckets in series. The first bucket has a leak rate of ρ_1 and a bucket size of β_1 . The second bucket has a leak rate of ρ_2 and a bucket size of $\beta_2=1$. Data enters from the left and flows through the buckets.

© R. Bettati

(x_{min} , x_{ave} , I_{ave} , s_{max}) model [Ferrari & Verma]

- x_{min} : minimum packet interarrival time
- x_{ave} : average packet interarrival time
- I_{ave} : averaging interval length
- s_{max} : maximum packet length

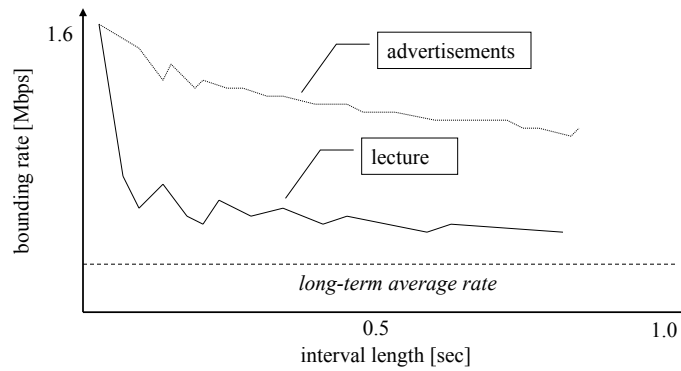
$$b(x_{min}, x_{ave}, I_{ave}, s_{max})(I) = \left(\min \left(\left\lceil \frac{t \bmod I_{ave}}{x_{min}} \right\rceil, \left\lceil \frac{I_{ave}}{x_{ave}} \right\rceil \right) + \frac{I}{I_{ave}} \right) s_{max}$$

The graph plots the worst case number of jobs/cells released against the number of jobs/cells I . The function consists of three segments: a linear segment with slope $1/x_{min}$ up to I_{ave} , a horizontal segment of length I_{ave} , and a linear segment with slope $1/x_{ave}$.

© R. Bettati

D-BIND [Knightly & Zhang]

- Other models do not accurately describe burstiness.
- Rate-interval representation:



- Model traffic by multiple rate-interval pairs: (R_k, I_k) , where rate R_k is the worst-case rate over every interval of length I_k .

© R. Bettati

D-BIND (2)

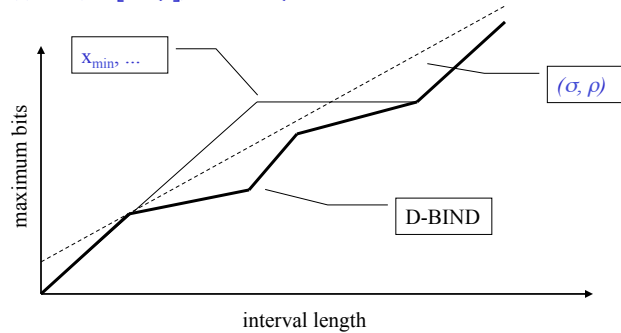
- Constraint function for D-BIND model with P rate-interval pairs:

$$b(t) = \frac{R_k I_k - R_{k-1} I_{k-1}}{I_k - I_{k-1}} (t - I_k) + R_k I_k, \quad I_{k-1} \leq t \leq I_k$$

$$b(0) = 0$$

$$b(t) = b(t - \lfloor t / I_p \rfloor) \text{ for } t > I_p$$

- Comparison:



© R. Bettati

Policing for the D-BIND Model

- Lemma:** If $b(t)$ is piece-wise linear concave, then R_k is strictly decreasing with increasing I_k .
- Lemma:** If a piece-wise linear constraint function $b(t)$ with P linear segments is concave, then the source may be fully policed with a cascade of P leaky buckets.

© R. Bettati

Delay Computation: Overview

- Delay computation for **FIFO server** with deterministically constraint input traffic:

$$d_{FIFO} = \max_{I > 0} \left\{ \sum b_i(I) - RI \right\} / R$$

© R. Bettati

End-to-End Analysis

- Traffic regulation: **reshape** traffic to adhere to traffic function.
- Alternative: **re-characterize** by accounting for burstiness added by queuing delays
 - where d_Y is delay on Server Y .
- Deterministic Case:

$$d^{e2e} = \sum_{X \in R} d_X$$

© R. Bettati

Real-Time Communication

- Integrated Services: Integration of variety of services with different requirements (real-time and non-real-time)
- Traffic (workload) characterization
- **Scheduling mechanisms**
- Admission control / Access control (policing)
- Deterministic vs. stochastic analysis
 - Traffic characterization
 - Performance guarantees
- Later we will
 - talk about real-time communication management in the real-world (intserv, some diffserv)
 - wrap up things with a theoretical framework (network calculus)

© R. Bettati

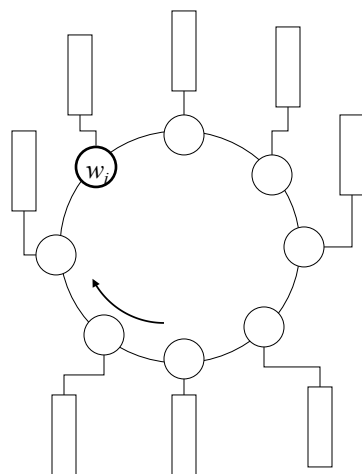
Switch Scheduling

- Work-conserving (greedy) vs. non-work-conserving (non-greedy) mechanisms.
- Rate-allocating disciplines: Allow packets to be served at higher rates than the guaranteed rate.
- Rate-controlled disciplines: Ensures each connection the guaranteed rate, but does not allow packets to be served above guaranteed rate.

- Priority-based scheduling:
 - fair queuing
 - virtual clock
 - earliest due date (EDD)
 - rate-controlled static priority (RCSP)
- Weighted Round-Robin scheduling:
 - WRR

© R. Bettati

Bit-by-Bit Weighted Round-Robin



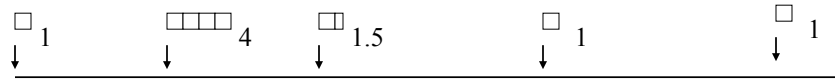
- bit-by-bit round robin
- each connection is given a weight
- each queue served in FIFO order

© R. Bettati

Fair Queueing [Demers, Keshav, Shenker]

- Emulate Bit-by-Bit Round Robin by prioritizing packets.
- Prioritize packets on basis of their finish time f_j :
 - a_j : arrival time of j -th packet
 - e_j : length of packet
 - f_j : finish time
 - BW : allocated fraction of link bandwidth

• Example: $f_j = \max(f_{j-1}, a_j) + e_j / BW$



- Complications:
 - What if connections dynamically change?

© R. Bettati

Guaranteed-Rate Scheduling Alg's [Goyal, Lam, Vin]

- **Guaranteed-Rate Clock** GRC associated with each packet. (intuitively, expected arrival time)
- Flow f is associated rate r_f (bits/sec)
- Let p_f^j and l_f^j denote j th packet of flow f and its length.
- $GRC^i(p_f^j)$: guaranteed-rate clock value of packet p_f^j
- $A^i(p_f^j)$: arrival time of packet p_f^j

$$GRC^i(p_f^0) = 0$$

$$GRC^i(p_f^j) = \max\{A^i(p_f^j), GRC^i(p_f^{j-1})\} + \frac{l_f^j}{r_f} \quad j \geq 1$$

- Examples are
 - Virtual-Clock
 - Packet-by-Packet Generalized Processor Sharing
 - Self-Clocked Fair Queueing
 - etc.

© R. Bettati

Virtual Clock Algorithm [L.Zhang]

- Emulate time-division multiplex (TDM) mechanism
 - Pre-allocation of slots eliminates interference among users.
- However:
 - TDM: when some connections idle, the slots assigned are idle
 - VC: idle slots are deleted from TDM frames
- auxiliary virtual clock ($auxVC_j$): finish time of j -th packet.
- virtual tick ($Vtick_j$): time to complete transmission of ready j -th packet.

$$Vtick_j = e_j / BW$$
- Replace f_j by $Vtick_j$; VC becomes identical to WFQ algorithm!
- Will look at delay analysis later.

© R. Bettati

Virtual Clock: Vanilla Implementation

1. Upon flow set-up of F_i with average transmission rate AR_i : compute value $Vtick_i = 1/AR_i$ (if variable-size packets, scale $Vtick$ appropriately)
2. Upon arrival of first packet from F_i : $VC_i := real_time$
3. Upon receiving packet j from F_i :
 - $VC_i := VC_i + Vtick_i$
 - timestamp packet j with value VC_i
4. Transmit packets in order of increasing VC 's
5. When switch runs out of buffer space, drop the last packet from the queue.

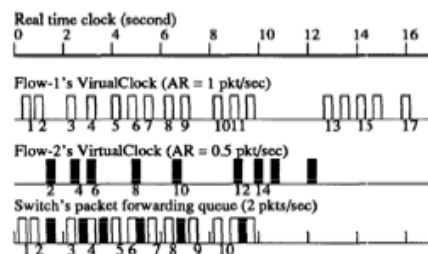
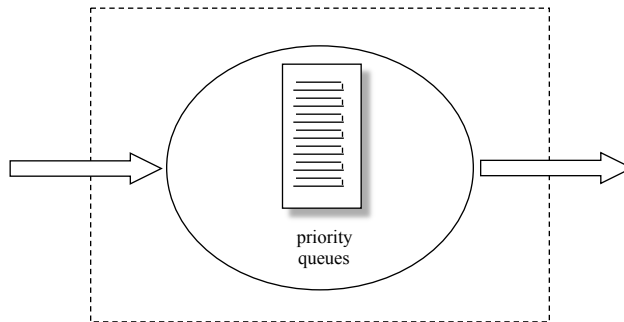


Figure 1: Real time, Virtual Clock, and packet processing order.

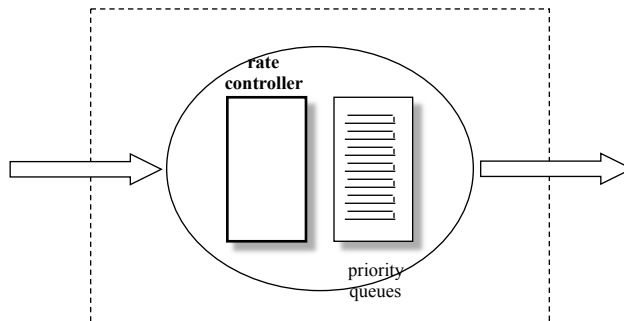
© R. Bettati

Rate-Controlled Static Priority (RCSP) [Zhang&Ferrari]



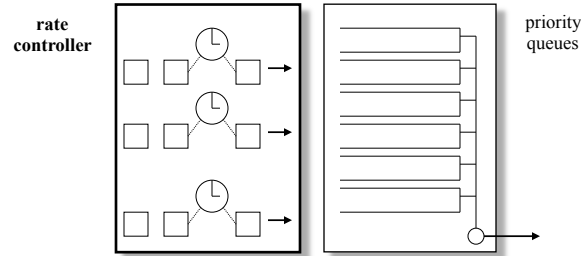
© R. Bettati

RCSP (2)



© R. Bettati

Traffic Regulation in RCSP



- Hold packets in regulator to guarantee minimum inter-packet arrival time.

$$r_{i,j} = \max(a_{i,j}, r_{i,j-1} + p_i)$$

- Implementation: buffer and timers in traffic regulator.
- Buffer requirements:

$$B_{ik} = \left(\left\lceil \frac{d_{ik}}{p_i} \right\rceil + \left\lceil \frac{d_{ik-1}}{p_i} \right\rceil \right) e_i$$

© R. Bettati

Is it Necessary to Regulate?

- [Liebeherr, Wrege, Ferrari, Transactions on Networking, 1995]
- Generalization of schedulability for arbitrary traffic constraint functions $b(I)$:

Theorem: A set N of connections that is given by $\{b_j, d_j\}$ is schedulable according to a static-priority algorithm if and only if for all priorities p , and for all $I \geq 0$ there is a t with $t \leq d_p - s_p^{\min}$ such that:

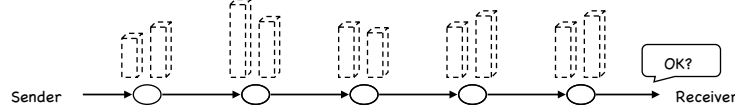
$$\forall I, \exists t \leq d_p - s_p^{\min} : I + t \geq \sum_{j \in C_p} b_j(I) - s_p^{\min} + \sum_{q=1}^{p-1} \sum_{j \in C_q} b_j((I+t)^-) + \max_{r>p} \{s_r^{\max}\}$$

© R. Bettati

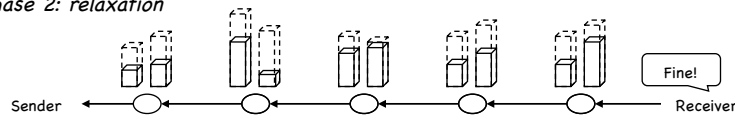
Earliest Due Date (EDD) [Ferrari]

- based on EDF
- delay-EDD vs. jitter-EDD
- works for periodic message models (single packet in period): $(p_i, 1, D_i)$
- partition end-to-end deadline D_i into local deadlines $D_{i,k}$ during connection establishment procedure.
- 2-Phase establishment procedure:

Phase 1: tentative establishment



Phase 2: relaxation



© R. Bettati

Delay EDD

- Upon arrival of Packet j of Connection i :
 - Determine effective arrival time: $a_{i,j}^e = \max(a_{i,j-1}^e + p_i, a_{i,j})$
 - Stamp packet with local deadline: $d_{i,j} = a_{i,j}^e + D_{i,k}$
 - Process packets in EDF order.
- Delay EDD is greedy.
- Can be mapped into special case of Sporadic Server.
- Acceptance test ($\Delta =$ total density): $\Delta + 1/p_i < 1 - 1/p_{min}$
- Offered local deadline: $LD_i = \min(p_i, 1/(1-\Delta-1/p_{min}))$
- Problem with EDD: **jitter**
 - **max** end-to-end delay over k switches: $\sum_k D_{i,k}$
 - **min** end-to-end delay over k switches: k

© R. Bettati

Jitter EDD

- Problem with Delay-EDD: does not control jitter. This has effect on buffer requirements.
- Jitter-EDD maintains **Ahead Time** $ah_{i,j}$, which is the difference between local relative deadline $D_{i,k-1}$ and actual delay at Switch $k-1$.
- Ahead time is stored in packet header (alternatively, we use global time synchronization)
- Upon receiving the j -th packet of Connection i with $ah_{i,j}$ at time $a_{i,j}$:
 - Calculate ready time as Switch k :

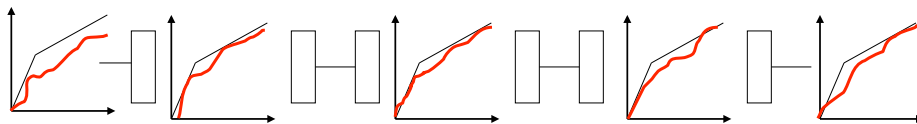
$$a_{i,j}^e = \max(a_{i,j-1}^e + p_i, a_{i,j})$$

$$r_{i,j} = \max(a_{i,j}^e, a_{i,j} + ah_{i,j})$$
 - Stamp packet with deadline $d_{i,j} = r_{i,j} + D_{i,k}$ and process according to EDF starting from ready time $r_{i,j}$.
- Result: Regenerate traffic at each switch.

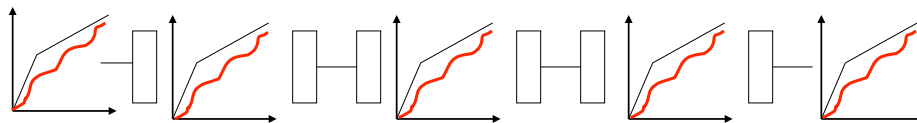
© R. Bettati

Rate Control vs. Jitter Control

- Rate Control



- Jitter Control



© R. Bettati

Simple EDF with Arbitrary Arrival Functions

[Liebeherr, Wrege, Ferrari: Transactions on Networking, 1995]

Theorem: A set Π of connections that is given by $\{b_j; d_j\}_{j \in \Pi}$ and $d_j \leq d_j$ whenever $i < j$ is EDF schedulable if and only if for all $I \geq d_j$:

where
$$I \geq \sum_{j \in \Pi} b_j(I - d_j) + \max_{k, d_k > I} \{s_k^{max}\}$$

$$\max_{k, d_k > I} \{s_k^{max}\} = 0 \text{ for } I > \max_{k \in \Pi} \{d_k\}$$

Informal “proof”: A deadline violation occurs at time I if the maximum traffic arrivals with deadline before or at time I exceeds I , i.e.:

$$I < \sum_{j \in \Pi} b_j(I - d_j)$$

© R. Bettati

EDF Test for Special Cases: Example (σ, ρ)

- For some traffic models, closed-form expressions for the schedulability test exist.
- For (σ, ρ) traffic:

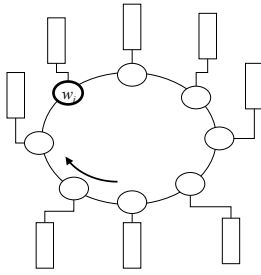
$$\left\{ \begin{array}{l} I \geq \sum_{i=1}^j \sigma_i + \rho_i(I - d_i) + \max_{k > j} \{s_k^{max}\} \text{ for } d_j \leq I < d_{j+1} : 1 \leq j < |\Pi| \\ I \geq \sum_{i=1}^{|\Pi|} \sigma_i + \rho_i(I - d_i) \text{ for } I > d_{|\Pi|} \end{array} \right.$$

- A closed form for the delay can be given as follows:

$$d_j = \frac{\sigma_j + \sum_{i=1}^{j-1} (\sigma_i - \rho_i d_i) + \max_{k > j} \{s_k^{max}\}}{1 - \sum_{i=1}^{j-1} \rho_i}$$

© R. Bettati

Weighted Round Robin (WRR)



- Each connection i is assigned a weight w_i , i.e., it is allocated w_i slots during each round.
- Slot: time to transmit maximum-sized packet.

- Traffic model:
 - periodic (p_i, e_i, D_i)
 - variable bit rate models possible
- Realizations:
 - greedy WRR
 - Stop-and-Go (SG)
 - Hierarchical Round Robin (HRR)

© R. Bettati

Throughput and Delay Guarantees

- Each connection i is guaranteed w_i slots in each rounds.
- Round length RL : upper bound on sum of weights (design parameter)

$$\sum w_i \leq RL$$
- Constraints:
 - 1. $RL \leq p_{\min}$
 - 2. $w_i \geq \left\lceil \frac{e_i}{\lfloor p_i / RL \rfloor} \right\rceil$
- Delays:
 - at first switch: $\left\lceil \frac{e_i}{w_i} \right\rceil RL$
 - downstream: once packet passes first switch, it is immediately eligible on switches downstream -> has to wait at most RL
 - => end-to-end delay through N switches:
$$W_i \leq (\lceil e_i / w_i \rceil + N - 1)RL \leq p_i + (N - 1)RL$$

© R. Bettati

Problems with Greedy WRR

- Greedy WRR does not control jitter:

	First Switch	
<ul style="list-style-type: none"> • min end-to-end delay: • max end-to-end delay: • jitter: 	$\begin{matrix} e_i \\ p_i \\ p_i - e_i \end{matrix}$	$\begin{matrix} +(N-1) \\ +(N-1)RL \\ +(N-1)(RL-1) \end{matrix}$

- Buffer needed at k -th switch for Connection i :

$$(1 + \lceil (k-1)(RL-1) / p_i \rceil) e_i$$

- Need traffic shaping at each switch.

© R. Bettati

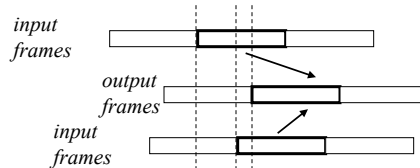
Non-Greedy WRR

- Actual length of rounds in greedy WRR varies with amount of traffic at switch.
- Non-greedy WRR schemes fix round length into fixed-length frames.
- Stop-and-Go [Golestani]
- Hierarchical Round Robin [Kalmanek, K., K.]

© R. Bettati

Stop & Go [Golestani, 1990]

- Frame-based: divide time in **frames** of length RL .
- Packet arriving during frame at input link is eligible for transmission during **next** frame on output link.



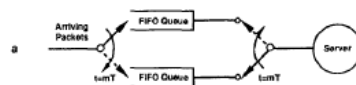
- Stop-and-Go is *not* work-conserving.
- Traffic model **(r, RL) smooth traffic**: during each frame of length RL , the total number of bits transmitted by source does not exceed rRL bits.

• **Proposition:** If the connection satisfies (r, RL) smoothness at the input of the first server, and each server ensures that packets will always go out on the next departing frame, the connection will satisfy (r, RL) smoothness at each server throughout the network.

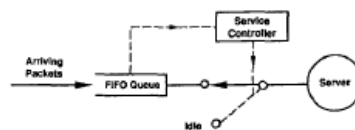
© R. Bettati

Stop & Go: Implementation

- Implementation of scheduler is not defined by Stop-and-Go frameworks.
- Implementation 1: FIFO scheduler with double-queue structure



- Implementation 2:



© R. Bettati

Multi-Frame Stop-and-Go

[For example, Zhang&Knightly: "Comparison of RCSP and SG", ACM Multimedia, 4(6) 1996]

- Problem with Stop-and-Go (or any other frame-based approach): **delay-bandwidth coupling**
 - Delay of packet is bounded by a multiple of frame time. This is a problem, for example for low-bandwidth, low-delay connections. (Why?)
- Solution: Use multi-level framing. Example:



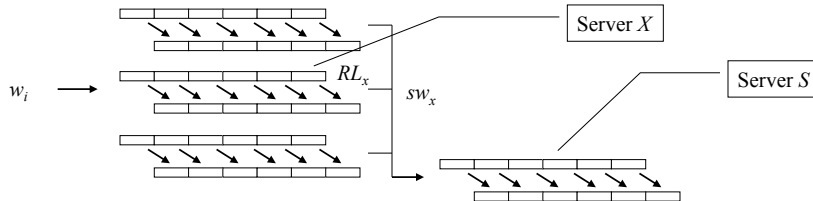
- Hierarchical framing with n levels with frame sizes RL_1, \dots, RL_n , where $RL_{m+1} = K_m RL_m$ for $m = 1, \dots, n-1$.
- Stop-and-Go rule for packets of level- p connection: Packets that arrived during a RL_p frame will not become eligible until the start of the next RL_p frame.
- Packets with smaller frame size have higher priority (non-preemptively) over packets with larger frame size.

© R. Bettati

Hierarchical Round Robin

[Kalmanek, Kanadia, Keshav, 1990]

- End-to-end delay and jitter of S&G depends on RL only.
- How about having multiple S&G servers, with different RL 's, and multiplex them on the same outgoing link?



- Server X is seen as periodic stream of requests by Server S , with
 - $e_x = sw_x$, $p_x = RL_x$, $D_x = RL_x$
 - schedule using rate-monotonic scheduler
 - Configuration time test: check whether task set $\{(sw_x, RL_x, RL_x)\}$ is schedulable.
- Admission Control Test:
 - Bandwidth test: check sum of required w_i 's $\leq sw_x$
 - Delay test: End-to-end delay: $p_i + N RL_x$
 - Jitter test: $2 RL_x$ with buffer requirement $2 w_i$

© R. Bettati