# The Role of Temporal Parameters in a Thalamocortical Model of Analogy

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*Abstract*—**How multiple specialized cortical areas in the brain interact with each other to give rise to an integrated behavior is a largely unanswered question. This paper proposes that such an integration can be understood under the framework of *analogy* and that part of the thalamus and the thalamic reticular nucleus (TRN) may be playing a key role in this respect. The proposed thalamocortical model of analogy heavily depends on a diverse set of temporal parameters including axonal delay and membrane time constant, each of which is critical for the proper functioning of the model. The model requires a specific set of conditions derived from the need of the model to process analogies. Computational results with a network of integrate and fire (IF) neurons suggest that these conditions are indeed necessary, and furthermore, data found in the experimental literature also support these conditions. The model suggests that there is a very good reason for each temporal parameter in the thalamocortical network having a particular value, and that to understand the integrated behavior of the brain, we need to study these parameters simultaneously, not separately.**

*Index Terms*—**Analogy, axonal delay, cortiothalamic feedback, membrane time constant, thalamic reticular nucleus, thalamus.**

## I. INTRODUCTION

UNDERSTANDING how cortical maps in the brain interact with each other to generate an integrated behavior is an important unsolved problem. Although we now know a lot more about the anatomical connectivity and physiology of the cortical maps than decades ago, such as layout of visual areas [1], [2] and long-range horizontal connectivity [3], [4], we still lack the understanding of how these maps work as an integrated system to give rise to a coherent behavior.

One key insight, from recent advances in neuroscience, can be gained from the thalamus. The thalamus is a centrally located nucleus in the brain with a high degree of feedforward and feedback connections to and from the cortex [5]–[7]. The thalamus was previously thought of as a passive relay station for sensory-motor signals. However, this explanation was not satisfactory once the existence of massive feedback from the cortex and a thin inhibitory network covering the thalamus called the thalamic reticular nucleus (TRN) [8] came to be known.

Several different functions have been attributed to the thalamus and its associated structures: 1) attentional modulation [9]–[11]; 2) predictive preactivation [12]; 3) temporal binding for perceptual coherence [13], [14]; 4) crossmodal modulation [15]; 5) active blackboard (or global workspace) [16]–[18]; 6) modulation of sleep and wake states [19], [20]; 7) action selection [21]; 8) mediation of cortico-cortical communication [22]; and 9) consciousness and awareness [23]–[26]. Although these explanations sound very different from each other, at the core they share a common theme that the thalamus integrates and/or selectively directs information received from the sensory periphery and also from the cortex. This insight is due to the massive convergence of both afferent and cortical feedback on to the thalamus (which is supposed to integrate diverse information), and also due to the inhibitory network surrounding the thalamus (i.e., the TRN, which performs selection, filtering, or gating). However, *what* gets integrated or selectively directed, or *what* is the property or nature of that which gets integrated or directed remains a question. For example, to what and to where does attention or prediction get directed, and how can these processes be generally characterized?

One possible answer to such a question of property (or content) of integration and gating in the thalamus is that part of the thalamus-TRN-cortex loop may be supporting a primitive form of analogical function (*analogy hypothesis* [27], [28]). In this sense, the analogy hypothesis does not attempt to replace the previous theories of thalamic function such as attention and prediction (as previously shown), but instead provides insights into the nature of such attention and prediction (see Section VII for more discussion on this point).

Analogy, defined broadly, plays an important role in human perception, cognition, and language [29]–[35], and in a more general sense, in motor control as well [30], [36]. The ability of analogy to cross domain boundaries is critical in these functions, and this may be exactly what is needed for the integrative operation of cortical maps. Relating one sensory modality (e.g., sound) to another (e.g., vision), explaining a more abstract concept in terms of more concrete sensory-motor concepts, and imitation of visually perceived events to generate a similar motion are all good examples where a broader definition of analogy can be applied, and where cortical integration is needed.

There is experimental evidence suggesting that the thalamus and the TRN may in fact be involved in an integrative activity (that can possibly be seen as a form of analogy). For example, Crabtree and Isaac [15] discovered through electrophysiological methods that there exists a rich set of functional pathways between different pairs of thalamic nuclei with different sensory cognitive motor modalities. More specifically, they showed that electrical stimulation of one nucleus in the dorsal thalamus can result in an inhibitory response in another nucleus of a different modality. These crossmodal influences are mostly inhibitory (GABAergic), and this is consistent with the view that the TRN

may take part in such an interaction by conducting disynaptic inhibition [15]. These results can provide experimental grounds for the analogy hypothesis, which puts an emphasis on the cross-modal function of the thalamus and the TRN.

Another important aspect of the thalamic function, besides the functional connectivity, is the diverse structural and physiological characteristics that can give rise to a complex temporal dimension to the functioning of this nucleus. For example, long membrane time constants in TRN neurons [37], [38], long axonal conduction delay in corticothalamic feedback due to the unmyelinated axons [39], and fast synaptic transmission between reticular neurons through gap junctions [40] are experimental results evidencing the rich temporal aspect of the thalamocortical network. In this paper, the role of this diversity in the temporal dimension will be investigated in relation to the function of analogy.

This paper presents a computational implementation of the hypothetical model described in [27] and [28] and compare the results with the previous predictions. The predictions are related to the various temporal requirements of the model and the goal is to show that the temporal dynamics we observe in experimental data have an important role to play under the framework of analogy.

Sections II–VII will briefly summarize the analogy hypothesis, then provide details of the implemented model, together with the results. The paper will conclude with a discussion about issues to be resolved, relevant related work, and future directions.

## II. ANALOGY THROUGH ASSOCIATIVE COMPLETION AND FILTERING

To motivate the thalamocortical model of analogy, let us first consider an abstract example which highlights two mechanisms that can together give rise to a simple form of analogy: completion and filtering [27], [28]. Completion is necessary for activating representations related to a certain given input and filtering is necessary for removing irrelevant ones among those completions.

Let us suppose that we have a simple brain with neurons (or populations of neurons) responding to specific inputs in the environment (Fig. 1). The simple brain has detectors for different input features including fruit objects (apple and orange), colors (red and orange color), and spoken words (the words red and orange). Note that each feature detector does not have to be a single neuron and it can be represented by a population of neurons, thus, forming a distributed representation (see Section VII). A neuron (or a distributed population) representing a certain feature will *invoke* other neurons (or populations) when they fire, and the invoking is done through relational (or associative) links which are supposed to be learned through experience and embody frequently co-occurring events or stimulus pairs. For example, the apple-object detector may have a strong connection to the color-red detector because apples are mostly red.

Given the above, consider the proportional analogy question `apple : orange :: word-red :?`. Fig. 1 shows an activation sequence of the simple brain to this input question. Initially, the first five neurons in the left are activated in response to this input [Fig. 1(a)]. Note that when an apple (object) is presented, it's red color also activates the color-red detector, and the same goes for the orange (object). Next, through the relational links, other cortical neurons are invoked [Fig. 1(b)]. This is where the *comple-*
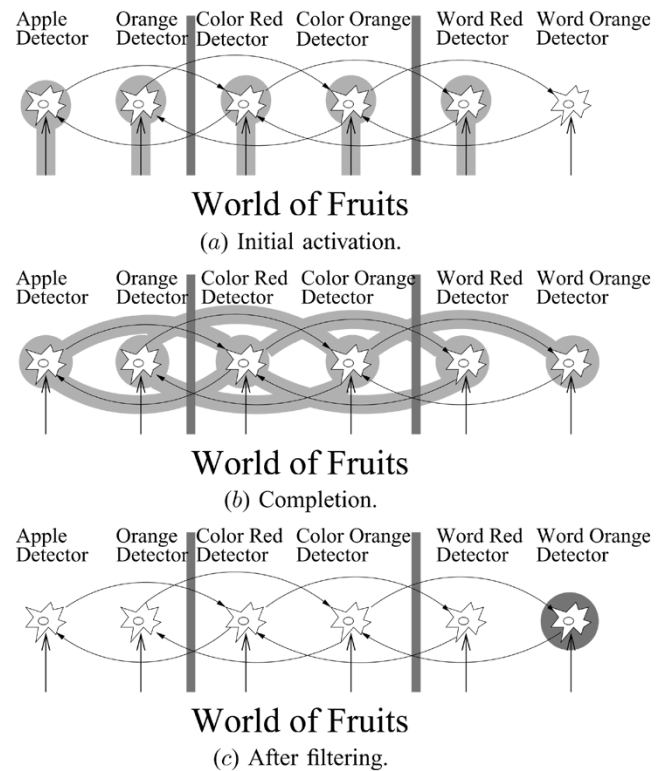


Fig. 1. Analogy through completion and filtering. A simple brain with six detector neurons is shown. Environmental input comes in from the bottom (*world of fruits*) and the neurons are linked with directed arcs that show the learned association between the detectors. The gray vertical bars partition the neurons into separate maps: object, color, and word maps from the left to the right. From (a) to (c) shows the activation sequence of the brain in response to an analogy question "`apple : orange :: word-red :?`." (a) Initial activation. (b) Associative completion across relational links. (c) Remaining activity after filtering out input-driven cortical activity.

*tion* occurs based on previously learned associations. It is like a replaying of the previously observed sequence of events, thus, it can be seen as *predicting* what is to be expected next, given the current input. Last, after *filtering* for the purely cortex-driven activity in the cortex as suggested in [27] and [28], only the word-orange detector remains active [Fig. 1(c)]. In other words, the filtering process promotes newly formed activity, not directly caused by the input, but somehow related to the current input. Interestingly enough, such a cortex-driven activity that survives the filtering (in this case `word-orange`) happens to be precisely the answer to the analogy question we previously posed. Thus, in this simple case, associative completion and filtering can account for a *primitive* form of an analogical process.

However, things can get complicated when combinations of objects are used in the question. Let us extend the simple brain to include concepts of small and big (not shown in Fig. 1). For such a case, simple filtering for only purely cortex-driven activity is insufficient because the answer can contain items that are already present in the question. For example, consider the analogy question a `big apple : small apple :: big orange :?`. The answer is `small orange`, but both `small` and `orange` appeared in the question, thus, the simple filtering as above will not work (i.e., everything will be filtered out). In this case, relaxing the filtering criterion allows us to get to the answer. Find *relatively less input-driven* cortical activities [27], [28] within each map (e.g., object map, color map, and word map shown in Fig. 1 divided by
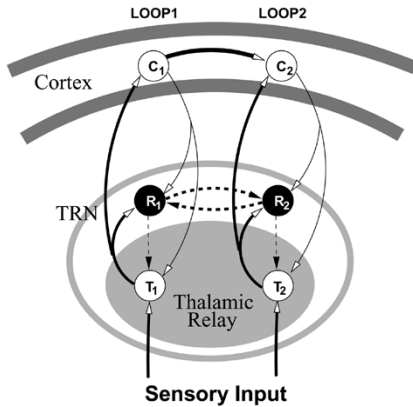
Fig. 2. Thalamocortical network. A schematic diagram of the thalamocortical network is shown (see [6] for a review). Solid edges with open arrows are excitatory connections and dashed edges with closed arrows are inhibitory connections. The thalamus is a centrally located nucleus in the brain and the dorsal part of it is covered with an inhibitory network of neurons called the TRN. Ascending and descending connections all branch out and stimulate reticular neurons, and the reticular neurons send inhibitory connections to the thalamic relay neurons. Two thalamocortical loops, Loop1 ($T_1$-$R_1$-$C_1$) and Loop2 ($T_2$-$R_2$-$C_2$), are shown. The two loops are connected to each other in the cortex and within the TRN.

the gray vertical bars). Following a similar activation sequence as in Fig. 1, we can see that `word-red` and `word-orange` are the purely cortex-driven activities. In addition, because `big` and `apple` appeared in the input twice but `small` and `orange` appeared only once, the latter two can survive the filtering under the new criterion. Thus, even for cortex-driven activities that are also input driven, those that are less input driven can survive and the correct analogical response can still be found among such activities that are more cortically-driven within each map (or area). Note that not only `small orange` survives such a filtering, and thus, the answer is not exact. However, what is more important here is that such a simple filtering process can generate a small set of *potential answers*. Although simple analogical questions may have straightforward answers, in more complex analogical problems, there can be multiple answers depending on the context [41], [42], and the flexibility shown above can be a desirable thing to have.

In summary, the examples demonstrated that simple analogies can be processed by completion and filtering. However, the proposed mechanism may not be able to account for more complex analogies, and other mechanism may also exist (see, e.g., [43]), but those are beyond the scope of the current paper. (See Section VII for further discussion on this point.) In Section III, we will see how the cortico-cortical connections and the thalamocortical circuit can exactly implement such a completion and filtering mechanism.

## III. ASSOCIATIVE COMPLETION AND FILTERING IN THE THALAMOCORTICAL LOOP

Previous papers proposed that the thalamus, TRN, and the associated part of the cortex may be involved in completion and filtering [27], [28]. Fig. 2 shows a schematic diagram of the thalamocortical circuit based on known anatomy and physiology [6], [15]. In the following, we shall review how this circuit can carry out completion and filtering.

Cortico-cortical connections linking different maps in the cortex are ideally suited for associative completion (see, e.g., [44]). Specific patterns of connections observed in animals (e.g., visual cortex of monkeys [4], [45]) show how such patterns can implement specific completion functions. Depending on how complex the representations are at the source and the target areas, and on how the actual cortico-cortical connections are wired, such pattern completions can give rise to a rich set of second-order activity in the cortex, in response to the sensory-driven first-order activity. The generated activity can be the result of logical inference, computation, memory recall, etc., but as shown in Section II, analogy is one reasonable (and important) candidate.

A more difficult issue is how filtering can be done, i.e., how can input-driven cortical activity be distinguished from cortex-driven cortical activity? As suggested in [27] and [28], the TRN is a promising location where such a filtering can occur. The basic idea is that the reticular neurons receive both ascending thalamic input- and descending-cortical feedback, and reticular inhibition cancels out cortical feedback to the thalamic relays when both ascending and descending spikes are received at the TRN. On the other hand, when only descending (i.e., corticothalamic) feedback is received, TRNs inhibition on the thalamic relay is weak and the relay neuron is allowed to fire in response to the cortical feedback, thus, invoking the cortical neuron for the second time around.

Fig. 3 shows a detailed activation sequence of this mechanism. The example shows a case where only one of the thalamocortical loops (Loop1) received sensory input, thus, demonstrating how *purely cortex-driven* activity can be promoted. The cortical feedback to the thalamus that survives the filtering is allowed to reactivate the cortex.

As for promoting the *relatively less input-driven* activity, we can think of a case when Loop1 receives a strong sensory input and Loop2 receives a weak sensory input. This time, both reticular neurons $R_1$ and $R_2$ will be highly activated, but due to the *disinhibition* (inhibition of an inhibitory neuron results in less inhibition at the target neuron) between the two, $R_2$ (which is strongly inhibited by $R_1$) cannot cancel out cortical feedback from $C_2$ to $T_2$. On the other hand, $R_1$, with its strong activity, will cancel out feedback from $C_1$ to $T_1$.

The description of the procedure sounds straightforward, but in fact, there are hidden assumptions (mostly regarding the temporal aspect) that are not quite obvious from the above. Section IV will explicate these hidden assumptions and provide theoretical (or functional) and experimental justifications for them.

## IV. FUNCTIONAL REQUIREMENTS OF THE PROPOSED MODEL

As mentioned above, there are specific assumptions that need to hold for the scenario described in Section III to work (see, e.g. Fig. 3):

1) reticular neurons must have slow dynamics [Fig. 3(b)–(d)];
2) inhibition between reticular neurons must be strong [Fig. 3(e)];
3) either the cortico-cortical connections must be very fast or the corticothalamic feedback connections must be slow (or both), compared to each other [Fig. 3(c) and (d)]; and
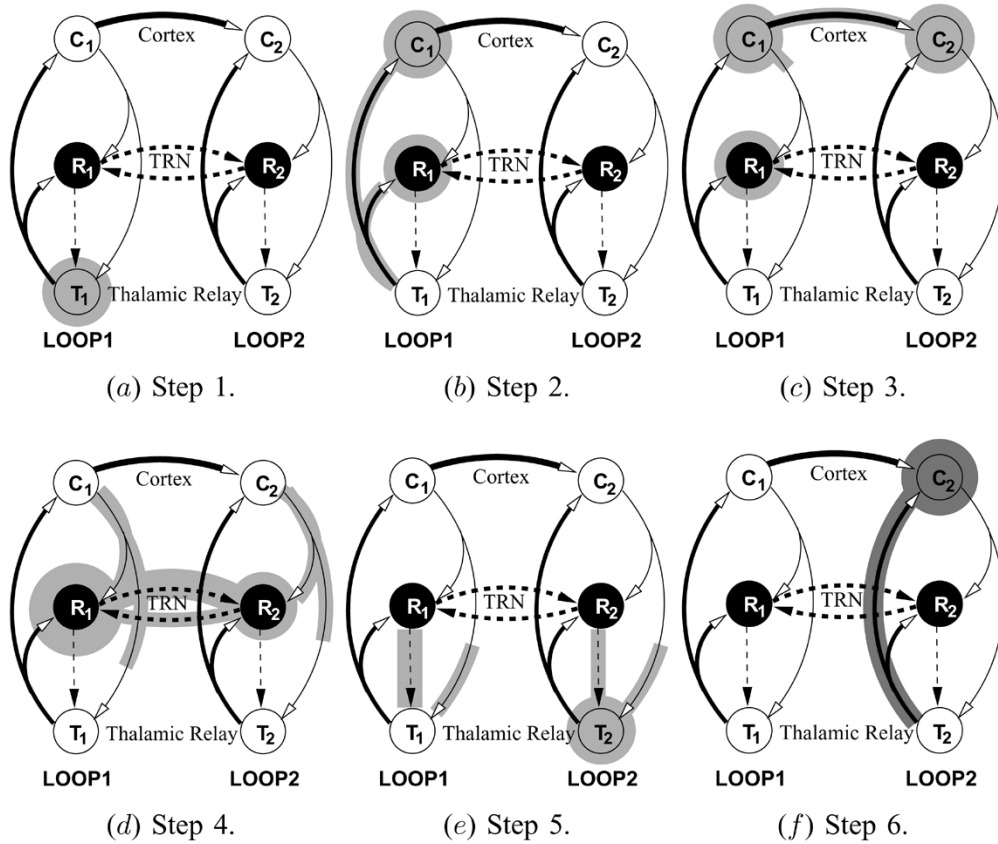
Fig. 3. Analogical completion and filtering in the thalamocortical circuit. An activation sequence of two thalamocortical loops (Loop1 and Loop2) are shown. Active parts of the circuit at each step are highlighted. (a) Initially, only $T_1$ receives an afferent sensory input. (b) $T_1$ invokes $R_1$ and $C_1$. (c) The cortical neuron $C_1$, through fast connections, invokes another cortical neuron $C_2$. $C_1$ also sends out feedback to $R_1$ and $T_1$, but these connections are slow and the spike can only travel a short distance in the same time. Note that $R_1$ retains the level of excitation because of its slow dynamics. (d) Cortical feedback from both $C_1$ and $C_2$ arrives at the TRN, and adds to the existing activity at TRN. Reticular neurons $R_1$ and $R_2$ inhibit each other through fast connections. (e) At the time the cortical feedback arrives at $T_1$ and $T_2$, the reticular neurons exert inhibition on the thalamic relays. $R_1$, driven by both afferent input- and cortical-feedback exerts strong inhibition on $T_1$, effectively canceling out the cortical feedback from $C_1$. On the other hand, $R_2$ was only driven by the cortical feedback, and it is not enough to cancel out feedback from $C_2$ at the thalamic relay $T_2$. Thus, $T_2$ is permitted to fire again. As a result, $C_2$ will be the only active neuron in the cortex in the next iteration.

4) interaction between reticular neurons must be fast [Fig. 3(d)].

These conditions must hold due to the following functional requirements of the proposed model (in the same order as above):

1) reticular neurons need to retain the ascending excitation level to strongly inhibit the thalamic relay later when the cortical feedback comes around [$R_1$ in Fig. 3(b)–(d)];
2) reticular activity must not be strong enough to cancel out cortex-driven cortical feedback to the thalamic relay [$R_2$ in Fig. 3(e)];
3) both input-driven cortical activity $(C_1)$ and cortical activity $(C_2)$ driven by that input-driven cortical activity must send feedback to the thalamus and TRN at approximately the same time [Fig. 3(c) and (d)]; and
4) reticular neurons must rapidly adjust their activity level before inhibiting the thalamic relays [$R_1$ and $R_2$ in Fig. 3(d)].

Most of these conditions were described in [27] and [28], but some of those that were only implicit in the earlier description are made more explicit here.

As it turns out, all of these conditions have experimental support (in the same order as above):

1) reticular neurons activate and deactivate on a slow timescale compared to thalamic relays [37], [38];
2) reticular neurons are harder to depolarize than thalamic relays [38], which may be due to inhibition between reticular neurons;
3) corticothalamic feedback connections are unmyelinated (i.e., very slow) [39]; and
4) gap junctions have been found between reticular neurons [40], suggesting that the interaction between reticular neurons may be rapid.[1]

In the following, the conditions listed above will be tested in a computational implementation of the model.

## V. MODEL DESCRIPTION

A network of leaky integrate and fire neurons [46] was constructed to test the *analogy hypothesis* summarized in Section IV.

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[1]It is controversial whether gap junctions can directly carry out disinhibition as required in here. However, the existence of gap junctions shows that reticular neurons need to communicate at a high speed, suggesting that other connections between reticular neurons may have to be fast as well.

Six neurons of three types: thalamic relay (T), thalamic reticular neuron (R), and cortical neuron (C) were connected according to the diagram in Fig. 2 (with the additional reciprocal connection from $C_2$ to $C_1$). For each neuron $i$, the membrane potential $V_i$ evolved according to the following dynamic equation:

$$C_i \frac{dV_i}{dt} = I_i(t) - \frac{V_i}{R_i} \qquad (1)$$

where $C_i$ is the membrane capacitance, $R_i$ the resistance, and $I_i(t)$ the input contribution to neuron $i$ at time $t$. When $V_i$ reaches a threshold value $\theta_i$, a spike is generated and $V_i$ is reset to the baseline (0.0). A spike generated by a presynaptic neuron $j$ results in a postsynaptic potential (PSP) $s_{ij}$ at a target neuron $i$, which is set to 1.0 at the moment the spike is received and is decayed over time as follows:

$$\frac{ds_{ij}}{dt} = -\frac{s_{ij}}{\tau_i} \qquad (2)$$

where $\tau_i$ is the membrane time constant of the PSP of the neuron $i$. The input contribution $I_i(t)$ to the neuron $i$ at time $t$ is defined as follows:

$$I_i(t) = \sum_{j \in \mathcal{N}_i} w_{ij} s_{ij}(t - \delta_{ij}) \qquad (3)$$

where $\mathcal{N}_i$ is the set of neurons sending spikes to neuron $i$ (see Fig. 2 for the connectivity); $w_{ij}$ is the connection weight from neuron $j$ to $i$ (the sign is negative if $j$ is an inhibitory neuron); and $s_{ij}(t - \delta_{ij})$ is the PSP generated in neuron $i$ by a spike from neuron $j$ with a conduction delay of $\delta_{ij}$ (see Tables I and II for the exact parameter values).

## VI. EXPERIMENTS AND RESULTS

Six experiments were conducted with the model previously described to test the assumptions and predictions in the hypothetical model [27], [28]. The common setup for these experiments is summarized in Section VI-A. The first three experiments (Sections VI-B–D) tested if the model tuned according to the conditions listed in Section IV can filter out input-driven or more input-driven cortical activity and just leave either the purely cortex-driven or relatively more cortex-driven activity in the cortex. The remaining experiments (Sections VI-E–G) systematically tested the effects of violated conditions on the function of analogy.

### A. General Experimental Setup

Tables I and II list the neuron and connection parameters (the units are arbitrary). The parameters are fairly uniform, except for the values in bold-type indicating a deviation from the default parameters. The deviations are not arbitrary, and are specifically required as discussed in Section IV (in the same order):

1) the membrane capacitance $C_i$ of a reticular neuron $R_i$ must be large ($= 0.6$, twice the default value) so that the membrane has slow dynamics;
2) the synaptic weight between reticular neurons $R_j$ to $R_i$ must be large ($= 10.0$, ten times the default value);

### TABLE I
NEURON PARAMETERS

| Parameter | Thal. Relay ($T_i$) | TRN ($R_i$) | Cortex ($C_i$) |
|---|---|---|---|
| Capacitance $C_i$ | 0.3 | **0.6** | 0.3 |
| Resistance $R_i$ | 3.0 | 3.0 | 3.0 |
| Threshold $\theta_i$ | 0.25 | 0.25 | 0.25 |
| PSP time constant $\tau_i$ | 0.05 | 0.05 | 0.05 |

### TABLE II
CONNECTION PARAMETERS

| Weight $w_{ij}$ | $T_i$ | $R_i$ | $C_i$ | Delay $\delta_{ij}$ | $T_i$ | $R_i$ | $C_i$ |
|---|---|---|---|---|---|---|---|
| $T_j$ | | 1.0 | 1.0 | $T_j$ | | 2.0 | 2.0 |
| $R_j$ | **2.0** | **10.0** | | $R_j$ | 2.0 | **0.2** | |
| $C_j$ | 1.0 | 1.0 | **0.9** | $C_j$ | **4.0** | 2.0 | **0.2** |

3) the conduction delay $\delta_{ij}$ from a cortical neuron $C_j$ to a thalamic relay $T_i$ must be large ($= 4.0$, twice the default value); the conduction delay $\delta_{ij}$ from a cortical neuron $C_j$ to another cortical neuron $C_i$ must be very small ($= 0.2$, one-tenth the default value); and
4) the conduction delay $\delta_{ij}$ from a reticular neuron $R_j$ to $R_i$ must be small ($= 0.2$, one-tenth the default value).

The two exceptions are the $R_i$ to $T_i$ connection weight ($= 2.0$, twice the default value) and the cortico-cortical connection weight ($= 0.9$, 90% of the default value). These parameters were found empirically and the significance of the relative magnitude of these parameters needs to be further investigated. A possible reason for $R_i$ to $T_i$ connection weight being high is that this inhibitory influence should be strong enough to cancel out input-driven cortical feedback. As for the cortico-cortical connection weight, it has to be lower than 1.0 to avoid a positive feedback loop that can potentially make the activity to go out of control.

The same set of parameters were used without modification in all the experiments, except for the following: 1) in Sections VI-C and D, where the $R_i$ to $T_i$ connection weight was increased; and 2) in Sections VI-E–G, the temporal parameters were altered to systematically test the effects of violated conditions.

### B. Experiment 1: Input-Driven Versus Cortex-Driven Activity in a Single Loop

To independently test the function of a *single* thalamocortical loop, depolarizing currents were injected at two different locations of the loop, the thalamic relay (T) and the cortical neuron (C), in two separate experiments. The thalamic injection emulated the input-driven condition and the cortical injection emulated the cortex-driven condition. The results are shown in Fig. 4.

In the input-driven case [Fig. 4(a)], the cortex activates at time $t = 3$ in response to the thalamic drive, but the corticothalamic feedback at time $t = 7$ is canceled out (i.e., filtered out) by
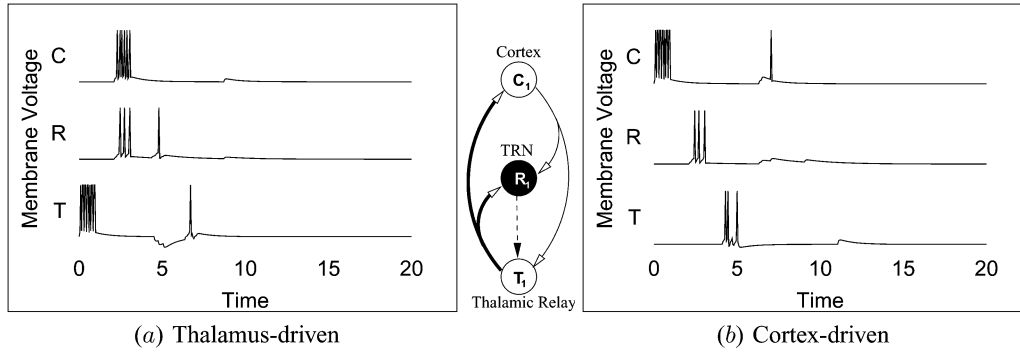
Fig. 4. Thalamus- versus cortex-driven activity. Membrane potential traces for a thalamic relay (T), a reticular neuron (R), and a cortical neuron (C) in a *single* loop are shown from the bottom row to the top row in each panel. The $x$ axis is time and the $y$ axis is the membrane potential. A depolarizing current of magnitude 1.0 and duration 1 was either injected in (a) the thalamic relay, emulating an input-driven condition, or in (b) the cortical neuron, emulating a cortex-driven condition. Only for the cortex-driven case (b), the initial cortical burst of activity can reactivate the cortical neuron through the corticothalamic loop ($t = 7$). Note that the plot shows the $V_i$ trace (1) with spikes added at the moment of threshold crossing. Also note that (a) and (b) are from two independent experiments.
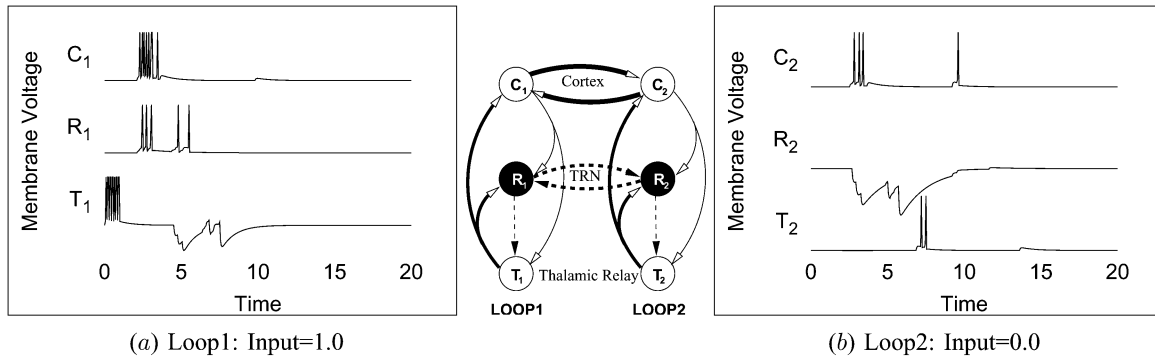


Fig. 5. Input versus no-input condition. Membrane potential traces for neurons in *two* connected thalamocortical loops are shown, one in (a) and the other in (b). The two loops are wired as shown in Fig. 2, with the addition of a reciprocal cortico–cortical connection from $C_2$ to $C_1$. The voltage traces for the neurons in the loops are numbered accordingly. (a) A depolarizing current of magnitude 1.0, duration 1 was injected in $T_1$. (b) No current was injected anywhere in the loop, thus, all activities were initially driven by the cortico-cortical connection from $C_1$ to $C_2$ at time $t = 3$. Only the cortex-driven cortical activity ($C_2$) is able to reactivate the cortex through feedback to the thalamus [$t = 10$ in (b)]. Note that the above are results from a single experiment, unlike in Fig. 4 where there were two.

the reticular inhibition. As a result, the cortical neuron fails to reactivate.

In contrast, for the cortex-driven case [Fig. 4(b)], the corticothalamic feedback to T at time $t = 5$ is strong enough to survive the weak reticular inhibition and successfully reactivates the cortex at time $t = 7$. These initial results demonstrate the ability of the model to perform filtering as discussed in Sections II and III.

### C. Experiment 2: Input Versus No-Input Condition in a Connected Pair of Loops

In this experiment, a pair of connected thalamocortical loops was simulated to test whether *purely cortex-driven* activity can survive the filtering in the model. The two loops were connected as in Fig. 2 with the addition of a reciprocal cortico-cortical connection from $C_2$ to $C_1$. To suppress hyperactivity in the thalamus caused by the strong feedback from the cortex due to this recursive cortico-cortical activation, the connection weight from $R_i$ to $T_i$ was increased to 5.0. All other conditions were identical to that of Section VI-B.

Input current was only injected into Loop1 thalamic relay $T_1$ to test the input (Loop1) versus no-input (Loop2) condition. The results are shown in Fig. 5. For the initially input-driven loop [Loop1 in Fig. 5(a)], the cortical burst of activity at time

$t = 3$ is unable to reactivate the cortex. However, for the initially cortex-driven loop [Loop2 in Fig. 5(b)], the cortical burst at time $t = 3$ induced by Loop1 is able to reactivate the cortex at $t = 10$ through the corticothalamic feedback. Thus, the model demonstrates selectivity for purely cortex-driven activity.

### D. Experiment 3: Strong- Versus Weak-Input Condition in a Connected Pair of Loops

The setup in this experiment was identical to Section VI-C, except for the input condition. For this experiment, Loop1 thalamic relay $T_1$ was injected with a depolarizing current of magnitude 2.0, and $T_2$ of Loop2 with a lower magnitude ($= 1.0$). Thus, a strongly input-driven versus weakly input-driven condition was setup to test whether *relatively less input-driven* cortical activity can be promoted in the model. The results are shown in Fig. 6.

The results are similar to those in Section VI-C. Cortical activity in the more input-driven Loop1 is unable to reactivate the cortex [Fig. 6(a)], but the less input-driven Loop2 is able to reactivate the cortex [$t = 10$ in Fig. 6(b)]. These results show that the model has selectivity for *less* input-driven cortical activity.

Note that in this case, disinhibition between reticular neurons serves an important role in allowing Loop2 to reactivate the cortex, despite the fact that Loop2 was also input-driven. Loop1
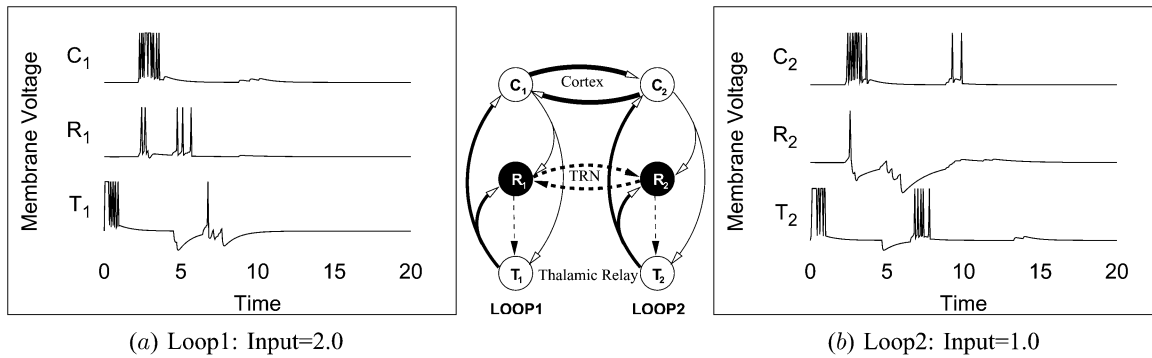
Fig. 6. Strong- versus weak-input condition. Membrane potential traces for two thalamocortical loops with an identical setup as in Fig. 5 are shown. The only difference was the magnitude of depolarizing current injected in loops 1 and 2. (a) A depolarizing current of magnitude 2.0, duration 1 was injected in $T_1$. (b) A depolarizing current of magnitude 1.0, duration 1 was injected in $T_2$. Thus, both loops were input-driven, but to a different degree. Only the less input-driven cortical activity $(C_2)$ is able to reactivate the cortex through feedback to the thalamus ($t = 10$ in b).
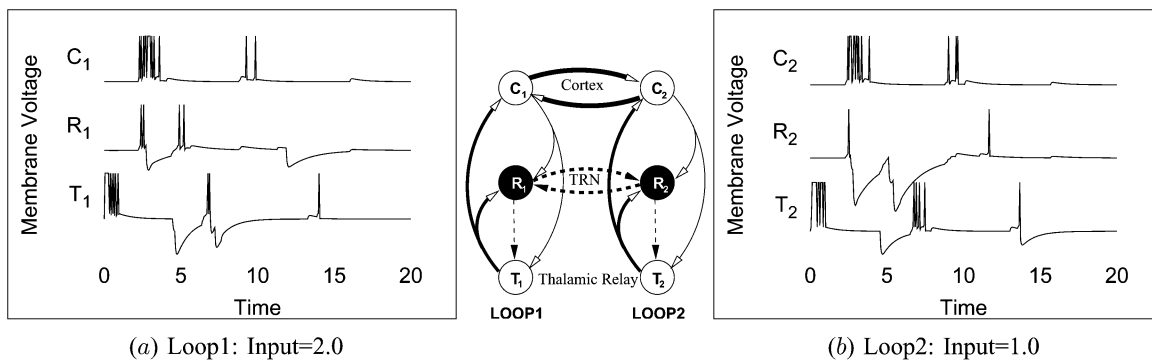


Fig. 7. Fast reticular-neuron dynamics. Membrane potential traces for two thalamocortical loops with an identical setup as in Fig. 6 are shown. The only difference was the lower membrane capacitance $(C_i = 0.5)$ in the reticular neurons $(R_i)$, which makes the membrane dynamics faster. The reticular neurons fail to integrate the thalamic and cortical contributions, and timely inhibition is interrupted.

reticular neuron $R_1$ fires more vigorously than $R_2$ of Loop2, and when they fire, they strongly inhibit $R_2$ [$t = 3$ and beyond in Fig. 6(b)], thus, weakening the inhibition exerted by $R_2$ on $T_2$. Compare this result to Fig. 5(a), where the same amount of input current injected in the thalamic relay resulted in the failure of the cortical neuron to reactivate.

The results suggest that relatively less input-driven cortical feedback can be detected and promoted in the proposed model, without changing any parameter (see, e.g., Section VI-C). In the following, we will see how violating model assumptions alter the behavior of the thalamocortical network.

### E. Experiment 4: Fast Reticular-Neuron Dynamics

Previously, in Section IV, we reasoned that the reticular neurons need to operate on a slow timescale because of the need to integrate both ascending thalamic contributions and descending cortical feedback. In this experiment, we will investigate the effect of faster reticular dynamics on the behavior of the model. The prediction is that analogical filtering, which depends on such an integration, will not work properly.

To test the effect, the capacitance of the reticular neurons was lowered to 0.2. All other simulation conditions were identical to that of Section VI-D. The resulting behavior, shown in Fig. 7, is a rapid activation and deactivation of the reticular neurons which causes the reticular neurons to fail to integrate the contributions from the ascending and feedback connections in a timely

manner. This leads to the failure of the reticular neurons to inhibit the thalamic relay neurons at the time cortical feedback arrives at the relay neurons (Fig. 7(a) at $t = 7$ and $t = 14$). Compared to Fig. 6, the firing of the thalamic relay neurons are markedly more robust, thus, it suggests that the reticular neurons are not performing the analogical filtering function properly. The results confirm that reticular neurons having a slow dynamics is important for integrating thalamic contribution and cortical feedback to perform analogical filtering.

### F. Experiment 5: Weak Synaptic Strength Between Reticular Neurons

If the reticular inhibition exerted on the thalamic relay neurons is too strong, cortical feedback can never survive the filtering at the thalamus whether or not that feedback was input driven or cortex driven. To ensure that the inhibition is not too strong, the reticular activity must not be too strong. For this, mutual inhibition within the TRN can play a significant role, and in Section IV, it was speculated that this inhibition should be strong. To test this prediction, the connection weight between the reticular neurons was decreased to 2.0. All other conditions were the same, as in Section VI-D.

The results are shown in Fig. 8. When we compare these results to Fig. 5 (where the intrareticular weight was high) we can notice that Loop2 fails to reactivate the cortex. This is because the reticular disinhibition was not strong enough to allow the $C_2$ to $T_2$ feedback to activate $T_2$ strongly enough. The results

(a) Loop1: Input=2.0                                                    (b) Loop2: Input=1.0
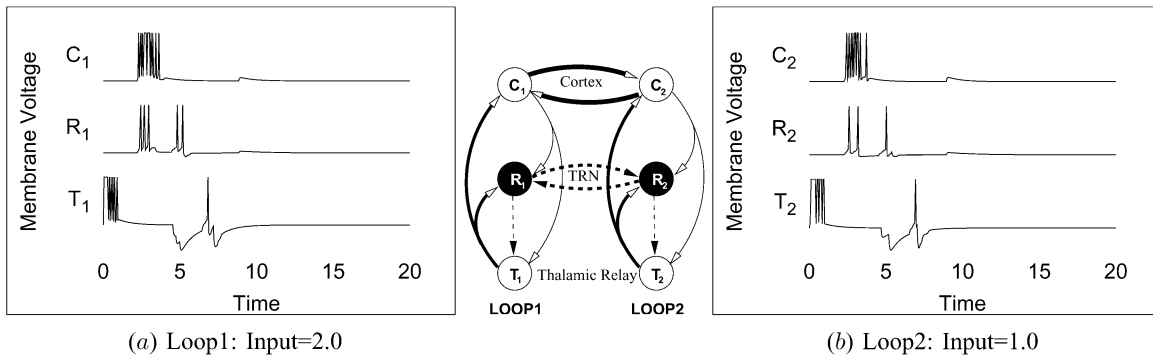
Fig. 8.   Weak synaptic strength between reticular neurons. Membrane potential traces for two thalamocortical loops with an identical setup as in Fig. 6 are shown. Only one parameter was altered: the connection weight between reticular neurons was decreased to 2.0. Due to the weaker disinhibition effect, Loop2 reticular neuron generates more activity to suppress the thalamic relay. As a result, Loop2 fails to reactivate the cortex.



(a) Loop1: Input=2.0                                                    (b) Loop2: Input=1.0
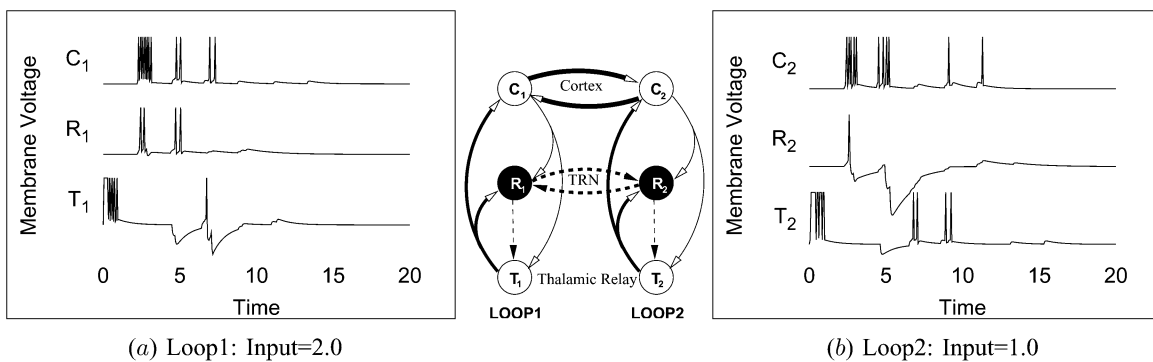
Fig. 9.   Longer cortico-cortical axonal delay. Membrane potential traces for two thalamocortical loops with an identical setup as in Fig. 6 are shown. The only difference was the cortico-cortical axonal delay, which was longer $(= 1.0)$. The result shows that the phases of Loop1 and Loop2 activities start to drift and become irregular.

suggest that reticular neurons need to inhibit each other strongly to satisfy the functional requirement of the analogy framework, and this can possibly be the reason why it is experimentally observed that reticular neurons are hard to depolarize [38].

### G. Experiment 6: Altered Delay Conditions

As shown in Section IV, the model requires specific delay conditions in two cases: 1) larger delay in corticothalamic feedback compared to cortico-cortical connections and 2) small delay between TRN neurons. In this section, the effect of violating these delay conditions will be investigated. Two experiments were conducted where all parameters were identical to those in Section VI-D, except for the particular delay condition being considered.

In the first experiment, the cortico-cortical connections were made slower $(= 1.0)$ so that the delay is similar to that of the thalamocortical feedback. Fig. 9 summarizes the results. Because of the longer delay in the cortex, the cortical feedback arrives at the thalamus out of sync with the reticular inhibition and this causes the tightly coupled behavior of the thalamocortical network to break down. For example, the cortical and thalamic activities beyond $t = 5$ in the two loops are out of phase.

On the other hand, in the second experiment, the axonal delay between reticular neurons within the TRN was made longer. As shown in Fig. 10, delayed inhibition within the TRN allows for a large amount of initial activity in the TRN $(t = 3$ to $t = 5)$, causing the reticular neurons to strongly inhibit the thalamic

relays. Because of this, the cortical feedback to the thalamic relays are totally suppressed $(t = 7)$. These two experiments show why the cortico-cortical connections and intra-TRN connections should be fast, if the analogy model is to properly function.

The results show that specific delays found in the thalamocortical network support analogical completion and filtering, and altering these delays can cause the function of analogy to break down.

### H. Summary of Results

In summary, the thalamocortical model functioned as predicted by the *analogy hypothesis*, with a set of parameters derived from functional, anatomical, and physiological considerations. The model was successful in detecting and promoting purely cortex-driven cortical activity and relatively less input-driven cortical activity, which forms the basis of the proposed model of analogical processing in the thalamocortical network (Section VI-B–Section VI-D).

Violated model assumptions regarding temporal parameters such as membrane time constant and axonal delay caused the model to fail to function properly as required by the framework of analogy (Section VI-E–Section VI-G). These results suggest that the temporal parameters found in experimental observations may have such specific values for a very good reason, i.e., to promote the processing of analogies through completion and filtering.
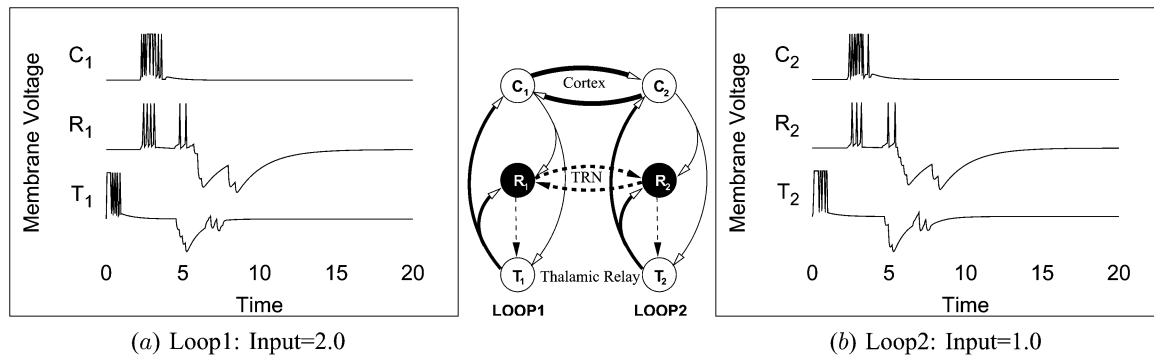
Fig. 10. Long axonal delay between reticular neurons. Membrane potential traces for two thalamocortical loops with an identical setup as in Fig. 6 are shown. All parameters were the same except for the delay between reticular neurons, which was increased to 1.5. Because of the delayed inhibition, the disinhibition effect did not happen in time to allow Loop2 to reactivate the cortex.

## VII. DISCUSSION

The main contribution of this paper was establishing a connection between analogy, thalamus and TRN, and temporal properties of neural circuits. Taken apart from each other, we can see that an enormous amount of research is going on in parallel in all of the three areas above. For example, in analogy research, several different perspectives have emerged: analogy as a higher level perception [31], [35], [36], analogy through structure mapping [47], analogy by constraint satisfaction [34], analogy using holographic representations [30], and a neural network theory of analogy [43] (see [43] for an extensive review of computational models of analogy). On the other hand, a separate line of research is going on in neuroscience where specific anatomical and physiological measures are gathered from the thalamus and its surrounding structures [5], [8], [12], [15], [19], [20], [22]. Based on these, various theories have been advanced, including attention, prediction, action selection, sleep/wake, and awareness and consciousness as discussed in Section I. The temporal properties of neurons and network of neurons are also heavily studied in both the experimental and the modeling and theory communities. Various temporal aspects of neuronal signaling are studied, such as the role of synchrony and resonance [14], [48]–[54], and how to understand and decode the temporal code of the neurons [55]. Although all of the three research areas above look rather unrelated at first, under the framework of analogy presented in this paper, things come together nicely and a coherent explanation becomes possible. If all parties involved can recognize the relevance of the developments in the other areas, a productive collaboration can be initiated.

The proposed model is not without limitations, realizing which naturally leads into several promising future directions. The first thing to notice is that the model produces a set of potential answers and not the exact answer, thus, further investigation may be necessary if the model is to be applied in solving more general analogy problems. Another limitation is that the model only supports a very constrained form of analogy, i.e., it is not able to deal with structural analogies [56]. To efficiently deal with structural analogies, the ordering of input and the role each input play must be taken into account, and for this, the involvement of the prefrontal cortex [57] and the hippocampus [58] must be assessed. As briefly discussed in

Section III, the complexity of the analogical mapping done by the thalamus-TRN-cortex loops depends on what is represented in the source and the target regions of the cortex, and how they are connected. For example, not just the objects or object properties, but object relations or case role can be represented in a spatially distributed manner in the (higher) cortical areas [30], [58], [59] and then a similar completion and filtering mechanism, as proposed in this paper, can be used to bring out the analogy.

The involvement of the prefrontal cortex leads to another question, about the role of higher order relays in the anterior thalamus [22]. Higher order relays do not receive any afferent input from the peripheral nervous system, which is quite distinct from the model in this paper. What would it mean to ask "what is the less input-driven activity?" in this case, when there is no input at all. It would be quite interesting to see how the model of analogy can be adjusted to that kind of anatomy (or if no adjustment is necessary at all).

A more general problem may be the simplistic notion of proportional analogy adopted by the model and the mechanism of completion and filtering that results. Certainly, analogy can go beyond the strict question–answer formalism, as discussed in Section I. Thus, the current model can only represent a limited part of the whole phenomenon of analogy. However, further experimental investigations into specific neural mechanisms of the thalamocortical circuit can potentially provide us with insights into new formalisms of analogy that can take us beyond this strict framework. Also, in terms of generalizing the approach, the possible applicability of the completion and filtering mechanism in other kinds of mapping can be explored, where completion performs a different kind of mapping (e.g., some form of inference), and filtering extracts the result of the mapping.[2]

Another limitation is the scale of the model. The maximum number of neurons used in the current study was only six. To study a larger scale behavior, scaling up is inevitable. This brings up another interesting point. In the current model, each loop consisting of individual neurons took on a specific function (a localist representation), but it is also possible to have synchronized populations of thalamocortical loops serve the role of a single loop (thus, forming a distributed representation). The thalamus also plays a critical role in modulating synchrony

[2]This last point is due to L. Shastri. See, also, Section III.

in the cortex [13], [60], and these synchronized populations can be formed and used as a higher level abstraction of a single thalamocortical loop. Instead of one localist neuron exciting another localist neuron, a distributed pattern can trigger (or complete) a different pattern (cf. synfire chains [61], [62]). The same thalamic mechanism can then perform filtering on these distributed, synchronized representations. This way, the model can be extended to work in a distributed parallel manner.

The model raises another question. If the primary function of the cortico-cortical and the thalamocortical network is to perform analogies, where does the rest of the perceptual, cognitive, and motor functions fit in? The cortex consists of more intricate microcircuits than illustrated in this paper, and certainly there are other subcortical nuclei (such as the hippocampus or the basal ganglia) connected to the cortex that serve functions other than analogy. Since the model presented in this paper only accounts for one part of what the cortex does, and only in relation to the thalamus, there is plenty of space left for other functional principles. In a similar manner, analogy may be only one part of the rich set of functions served by the thalamus, as those listed in the introduction. Certain anatomical features of the thalamus not included in the current model, such as the inhibitory interneurons and the "matrix" cells sending diffuse connections to layer I of the cortex [7] may be related to these functions other than analogy. Thus, the model presented in this paper is complementary, not contradictory, to the existing models of thalamus and cortex function.

Finally, we can derive several predictions from the model presented in this paper. The specific assumptions on connection weight and temporal parameters described in Section IV and the computational results already form a concrete prediction. Experiments similar to these can be conducted on live tissue blocks in vitro or even in vivo, and the course of activity in the thalamocortical network can be compared to the results presented in this paper. Also, one implicit assumption regarding the cortical feedback in the model was that the feedback alone (without sensory afferents) can activate the thalamic relay. For this to happen, the feedback has to have a driving influence (i.e., not just modulatory), but driver feedbacks are only known to exist in the higher order relays [5], [22]. However, the existence of such drivers in first-order sensory areas of the thalamus has not yet been disproven: The model predicts that driver feedback will also be found, and this may have to be experimentally verified in the future. The model also makes very specific predictions on the expected behavior when the normal parameters are disrupted (Section VI-E–Section VI-G). At a higher level, the model predicts that purely or more cortically driven activity in the cortex will reactivate while input-driven activity in the cortex will not reactivate. Experiments by Grill-Spector *et al.* partly confirms this prediction. They showed that elongated exposure to a same input caused the fMRI signature to decrease over time [63], [64]. A similar experiment can check if the fMRI responses for cortical activity *derived* from the immediate input are increased as predicted by the model. Whether the thalamus serves an analogical role can also be tested using fMRI devices while the subject is performing a cognitive task involving analogical abilities. Activities at the thalamus and the cortex can be measured simultaneously, and to get a better temporal resolution, elec-

troencephalogram (EEG) [or magnetoencephalogram (MEG)] studies can be done in parallel. Through such a study, cognitive scientists can gain new insights into a richer analogical mechanism through an understanding of the neural underpinnings of the process, and neuroscientists can better understand the function of the thalamocortical network, within the framework of analogy.

## VIII. CONCLUSION

In this paper, the thalamocortical model of analogy [27], [28] was tested computationally. A network of integrate and fire neurons was built and tuned based on functional, anatomical, and physiological considerations. The results showed that associative completion and filtering for less input-driven activity, which forms the basis of analogy, arise in the model. Various temporal parameters, tuned based on anatomical and physiological data, turned out to be crucial in enforcing the proper function of the model. This suggests that these parameters need to be studied together, not separately, under a general functional framework, such as the analogy model. One immediate future direction is to significantly scale up the model to include multiple cortical maps. The model can then be used to test whether the analogy framework can be generalized for the understanding of integration among multiple interacting cortical maps.

## ACKNOWLEDGMENT

## REFERENCES

[1] D. C. Van Essen, D. J. Felleman, E. A. DeYoe, J. Olavarria, and J. Knierim, "Modular and hierarchical organization of extrastriate visual cortex in the macaque monkey," in *Proc. Cold Spring Harbor Symp. Quantitative Biology*, vol. LV, Cold Spring Harbor, NY, 1990, pp. 679–696.

[2] D. C. Van Essen and H. A. Drury, "Structural and functional analyzes of human cerebral cortex using a surface-based atlas," *J. Neurosci.*, vol. 17, no. 18, pp. 7079–7102, 1997.

[3] C. D. Gilbert and T. N. Wiesel, "Columnar specificity of intrinsic horizontal and corticocortical connections in cat visual cortex," *J. Neurosci.*, vol. 9, pp. 2432–2442, 1989.

[4] W. H. Bosking, Y. Zhang, B. Schofield, and D. Fitzpatrick, "Orientation selectivity and the arrangement of horizontal connections in tree shrew striate cortex," *J. Neurosci.*, vol. 17, no. 6, pp. 2112–2127, 1997.

[5] S. M. Sherman and R. W. Guillery, *Exploring the Thalamus*. San Diego, CA: Academic, 2001.

[6] D. Mumford, "Thalamus," in *The Handbook of Brain Theory and Neural Networks*, M. A. Arbib, Ed. Cambridge, MA: MIT Press, 1995, pp. 153–157.

[7] S. Hill and G. Tononi, "Thalamus," in *The Handbook of Brain Theory and Neural Networks*, 2nd ed, M. A. Arbib, Ed. Cambridge, MA: MIT Press, 2003, pp. 1176–1180.

[8] J. W. Crabtree, "Intrathalamic sensory connections mediated by the thalamic reticular nucleus," *Cellular Molecular Life Sci.*, vol. 56, pp. 683–700, 1999.

[9] D. LaBerge, *Attentional Processing*. Cambridge, MA: Harvard Univ. Press, 1995.

[10] W. Kilmer, "A thalamo-cortical model of the executive attention system," *Biol. Cybern.*, vol. 84, pp. 279–289, 2001.

[11] F. Crick, "Function of the thalamic reticular complex: The searchlight hypothesis," in *Proc. Nat. Academy Sciences*, vol. 81, 1984, pp. 4586–4950.

[12] K. A. Moxon, G. Foffani, and J. K. Chapin, "Spatio-temporal shift of receptive field in thalamic reticular nucleus neurons of the rat," *Soc. Neurosci. Abstracts*, pp. 45.3–45.3, 2002.

[13] R. R. Llinás and U. Ribary, "Perception as an oneiric-like state modulated by the Senses," in *Large Scale Neuronal Theories of the Brain*, C. Koch and J. L. Davis, Eds. Cambridge, MA: MIT Press, 1994, ch. 6, pp. 111–124.

[14] R. Llinás, E. Ribary, M. Joliot, and G. Wang, "Content and context in temporal thalamocortical binding," in *Temporal Coding in the Brain*, G. Buzsaki, Ed. Berlin, Germany: Springer-Verlag, 1994.

[15] J. W. Crabtree and J. T. Isaac, "Intrathalamic pathways allowing modality-related and cross-modality switching in the dorsal thalamus," *J. Neurosci.*, vol. 22, pp. 8754–8761, 2002.

[16] D. Mumford, "On the computational architecture of the neocortex, pt. I, the role of the thalamo-cortical loop," *Biol. Cybern.*, vol. 65, pp. 135–145, 1991.

[17] J. Newman, B. J. Baars, and S.-B. Cho, "A neural global workspace model for conscious attention," *Neural Netw.*, vol. 10, pp. 1195–1206, 1997.

[18] E. Harth, K. P. Unnikrishnan, and A. S. Pandaya, "The inversion of sensory processing by feedback pathways: A model of visual cognitive functions," *Science*, vol. 237, pp. 184–187, 1987.

[19] M. Steriade and D. A. McCormick, "Thalamocortical oscillations in the sleeping and aroused brain," *Science*, vol. 262, pp. 679–685, 1993.

[20] D. A. McCormick and T. Bal, "Sleep and arousal: Thalamocortical mechanisms," *Annu. Rev. Neurosci.*, vol. 20, pp. 185–215, 1997.

[21] M. D. Humphries and K. N. Gurney, "The role of intra-thalamic and thalamocortical circuits in action selection," *Network: Computat. Neural Syst.*, vol. 13, pp. 131–156, 2002.

[22] R. W. Guillery and S. M. Sherman, "Thalamic relay functions and their role in corticocortical communication: Generalizations from the visual system," *Neuron*, vol. 33, pp. 163–175, 2002.

[23] C. M. Portas, G. Rees, A. M. Howseman, O. Josephs, R. Turner, and C. D. Frith, "A specific role for the thalamus in mediating the interaction of attention and arousal in humans," *J. Neurosci.*, vol. 18, pp. 8979–8989, 1998.

[24] J. G. Taylor, *The Emergent Mind*. Cambridge, MA: MIT Press, 1998.

[25] F. Crick, *The Astonishing Hypothesis: The Scientific Search for the Soul*. New York: Scribner, 1994.

[26] F. Crick and C. Koch, "Toward a neurobiological theory of consciousness," *Sem. Neurosci.*, vol. 2, pp. 263–275, 1990.

[27] Y. Choe, "Analogical cascade: A theory on the role of the thalamo-cortical loop in brain function," *Neurocomput.*, vol. 52–54, pp. 713–719, 2003.

[28] ——, "Second-order isomorphism: A reinterpretation and its implications in brain and cognitive sciences," in *Proc. 24th Annu. Conf. Cognitive Science Soc.*, W. D. Gray and C. D. Schunn, Eds., Fairfax, VA, 2002, pp. 190–195.

[29] G. Lakoff and M. Johnson, *Metaphors We Live By*. Chicago, : Univ. Chicago Press, 1980.

[30] P. Kanerva, "Dual role of analogy in the design of a cognitive computer," in *Advances in Analogy Research: Integration of Theory and Data From the Cognitive, Computational, and Neural Sciences*, K. Holyoak, D. Gentner, and B. Kokinov, Eds. Sofia: New Bulgarian Univ. Press, 1998, pp. 164–170.

[31] M. Mitchell, *Analogy-Making as Perception: A Computer Model*. Cambridge, MA: MIT Press, 1993.

[32] J. H. Holland, K. J. Holyoak, R. E. Nisbett, and P. R. Thagard, *Induction: Process of Inference, Learning, and Discovery*. Cambridge, MA: MIT Press, 1986.

[33] *The Analogial Mind: Perspectives from Cognitive Science*, D. Gentner, K. J. Holyoak, and B. N. Kokinov, Eds., MIT Press, Cambridge, MA, 2001.

[34] K. J. Holyoak and P. Thagard, *Mental Leaps: Analogy in Creative Thought*. Cambridge, MA: MIT Press, 1995.

[35] D. R. Hofstadter, *Fluid concepts and creative analogies: Computer models of the fundamental mechanisms of thought*. New York: Basic Books, 1995.

[36] C. T. Morrison, "Situated representation: Solving the handcoding problem with emergent structured representation," Ph.D. dissertation, Binghamton Univ., State Univ. New York, 1998.

[37] D. A. Coulter, J. R. Huguenard, and D. A. Prince, "Calcium currents in rat thalamocortical relay neurons: Kinetic properties of the transient, low-threshold current," *J. Physiol.*, vol. 414, pp. 587–604, 1989.

[38] J. R. Huguenard and D. A. McCormick, "A novel t-type current underlies prolonged $Ca^{2+}$-dependent burst firing in GABAergic neurons of rat thalamic reticular nucleus," *J. Neurosci.*, vol. 12, pp. 3804–3817, 1992.

[39] T. Tsumoto, O. D. Creutzfeldt, and C. R. Legendy, "Functional organization of the corticofugal system from visual cortex to lateral geniculate nucleus in the cat," *Exp. Brain Res.*, vol. 32, pp. 345–364, 1978.

[40] C. E. Landisman, M. A. Long, M. Beierlein, M. R. Deans, D. L. Paul, and B. W. Connors, "Electrical synapses in the thalamic reticular nucleus," *J. Neurosci.*, vol. 22, pp. 1002–1009, 2002.

[41] D. R. Hofstadter and M. Mitchell, "The copycat project: A model of mental fluidity and analogy-making," in *Advances in Connectionist and Neural Computation Theory*, K. J. Holyoak and J. A. Barnden, Eds. Norwood, NJ: Ablex, 1994.

[42] M. Mitchell, "Analogy-making as a complex adaptive system," in *Design Principles for the Immune System and Other Distributed Autonomous Systems*, L. Segal and A. Cohen, Eds. Oxford, U.K.: Oxford Univ. Press, 2001.

[43] N. G. Jani and D. S. Levine, "A neural network theory of proportional analogy-making," *Neural Netw.*, vol. 13, pp. 149–183, 2000.

[44] D. Mumford, "On the computational architecture of the neocortex, pt. II, the role of the cortico-cortical loop," *Biol. Cybern.*, vol. 65, pp. 241–251, 1992.

[45] G. G. Blasdel, "Orientation selectivity, preference, and continuity in monkey striate cortex," *J. Neurosci.*, vol. 12, pp. 3139–3161, Aug. 1992.

[46] F. Gabbini and C. Koch, "Principles of spike train analysis," in *Methods in Neural Modeling*, C. Koch and I. Segev, Eds. Cambridge, MA: MIT Press, 1999, ch. 7, pp. 313–360.

[47] D. Gentner, B. Bowdle, P. Wolff, and C. Boronat, *The Analogical Mind: Perpsectives from Cognitive Sciemce*, D. Gentner, K. J. Holyoak, and B. N. Kokinov, Eds. Cambridge, MA: MIT Press, 2001, pp. 199–253.

[48] W. Singer, "Synchronization of cortical activity and its putative role in information processing and learning," *Annu. Rev. Physiol.*, vol. 55, pp. 349–374, 1993.

[49] R. Eckhorn, R. Bauer, W. Jordan, M. Kruse, W. Munk, and H. J. Reitboeck, "Coherent oscillations: A mechanism of feature linking in the visual cortex?," *Biol. Cybern.*, vol. 60, pp. 121–130, 1988.

[50] C. M. Gray, P. Konig, A. Engel, and W. Singer, "Oscillatory responses in cat visual cortex exhibit inter-columnar synchronization which reflects global stimulus properties," *Nature*, vol. 338, pp. 334–337, 1989.

[51] D. L. Wang, "Emergent synchrony in locally coupled neural oscillators," *IEEE Trans. Neural Networks*, vol. 6, pp. 941–948, July 1995.

[52] G. B. Ermentrout and N. Kopell, "Fine structure of neural spiking and synchronization in the presence of conduction delays," in *Proc. Nat. Academy Sciences*, vol. 95, 1998, pp. 1259–1264.

[53] E. M. Izhikevich, "Resonate-and-fire neurons," *Neural Netw.*, vol. 14, pp. 883–894, 2001.

[54] ——, "Simple model of spiking neurons," *IEEE Trans. Neural Networks*, vol. 14, pp. 1569–1572, Nov. 2003.

[55] F. Rieke, D. Warland, R. de Ruter van Stevenick, and W. Bialek, *Spikes: Exploring the Neural Code*, 1st ed. Cambridge, MA: MIT Press, 1997.

[56] D. Gentner and A. B. Markman, "Analogy-based reasoning and metaphor," in *The Handbook of Brain Theory and Neural Networks*, 2nd ed, M. A. Arbib, Ed. Cambridge, MA: MIT Press, 2003, pp. 106–109.

[57] J. M. Fuster, *The Prefrontal Cortex: Anatomy, Physiology, and the Frontal Lobe*, 3rd ed. New York: Lippencott-Raven, 1997.

[58] L. Shastri, "Episodic memory and cortico-hippocampal interactions," *Trends Cognitive Sci.*, vol. 6, pp. 162–168, 2000.

[59] R. Miikkulainen, *Subsymbolic Natural Language Processing: An Integrated Model of Scripts, Lexicon, and Memory*. Cambridge, MA: MIT Press, 1993.

[60] A. M. Sillito, H. E. Jones, G. L. Gerstein, and D. C. West, "Feature-linked synchronization of thalamic relay cell firing induced by feedback from the visual cortex," *Nature*, vol. 369, pp. 479–482, 1994.

[61] M. Abeles, *Corticonics: Neural Circuits of the Cerebral Cortex*, 1st ed. Cambridge, U.K.: Cambridge Univ. Press, 1991.

[62] Y. Prut, E. Vaadia, H. Bergman, H. Haalman, I. Slovin, and M. Abeles, "Spatiotemporal structure of cortical activity: Properties and behavioral relevance," *J. Neurophys.*, vol. 79, pp. 2857–2874, 1998.

[63] K. Grill-Spector, T. Kushnir, S. Edelman, G. Avidan, Y. Itzchak, and R. Malach, "Differential processing of objects under various viewing conditions in the human lateral occipital complex," *Neuron*, vol. 24, pp. 187–203, 1999.

[64] K. Grill-Spector and R. Malach, "FMR-adaptation: A tool for studying the functional properties of human cortical neurons," *Acta Psychologica*, vol. 107, pp. 293–321, 2001.

[65] B. Ermentrout, *Simulating, Analyzing, and Animating Dynamical Systems: A Guide to XPPAUT for Researchers and Students*.   Philadelphia, PA: SIAM, 2002.

[66] Y. Choe, "Processing of analogy in the thalamocortical circuit," in *Proc. Int. Joint Conf. Neural Networks*, Portland, OR, 2003, pp. 1480–1485.

[67] *The Handbook of Brain Theory and Neural Networks*, 2nd ed., M. A. Arbib, Ed., MIT Press, Cambridge, MA, 2003.
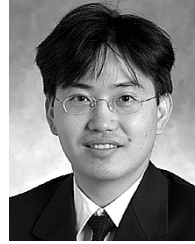
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