

**Challenge Problem 1**  
CPSC 489/689 Quantum Algorithms  
Andreas Klappenecker

The hidden subgroup problem can be informally stated as follows:

**The Hidden Subgroup Problem:** Let  $f: G \rightarrow X$  be a black box function from a finite group  $G$  to a finite set  $X$  such that

$$f(x) = f(y) \quad \text{if and only if} \quad y^{-1}x \in H,$$

where  $H$  is some initially unknown subgroup of  $G$ . Your task is to find a generating set  $S$  of  $H$ .

Find an *efficient* quantum algorithm, which solves the Hidden subgroup problem for all finite groups  $G$ . Alternatively, show that such an algorithm cannot exist.

I offer a **Challenges in Quantum Computing Award**, worth US\$ 256, for the first correct solution to this problem.

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