

$$\Pr \left[\bigcap_{j=1}^{n-2} E_j \right] \geq \prod_{m=1}^{n-2} \left(\frac{n-m-1}{n-m+1} \right) = \frac{2}{n(n-1)}.$$