

Lemma 2 *Let U be a unitary 2×2 matrix that is not a multiple of the identity matrix I . Then*

$$V = \frac{1}{\sqrt{\operatorname{tr} U \pm 2\sqrt{\det U}}} (U \pm \sqrt{\det U} I)$$

is a unitary matrix satisfying $U = V^2$.